

SLIDING DARK MATTER AND PHENOMENOLOGY

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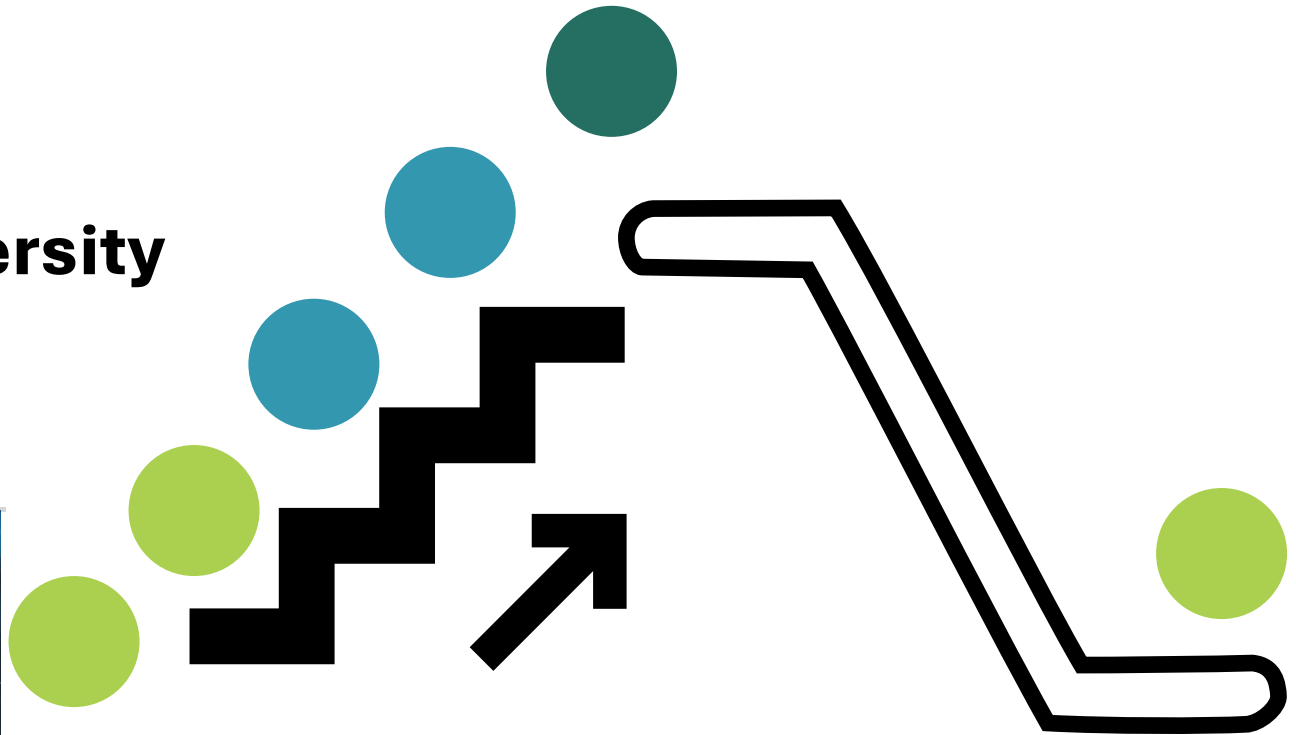
Nanjing Normal University

Jun.18, 2026

紫金山暗物质研讨会

新疆·乌鲁木齐

2026年7月20-25



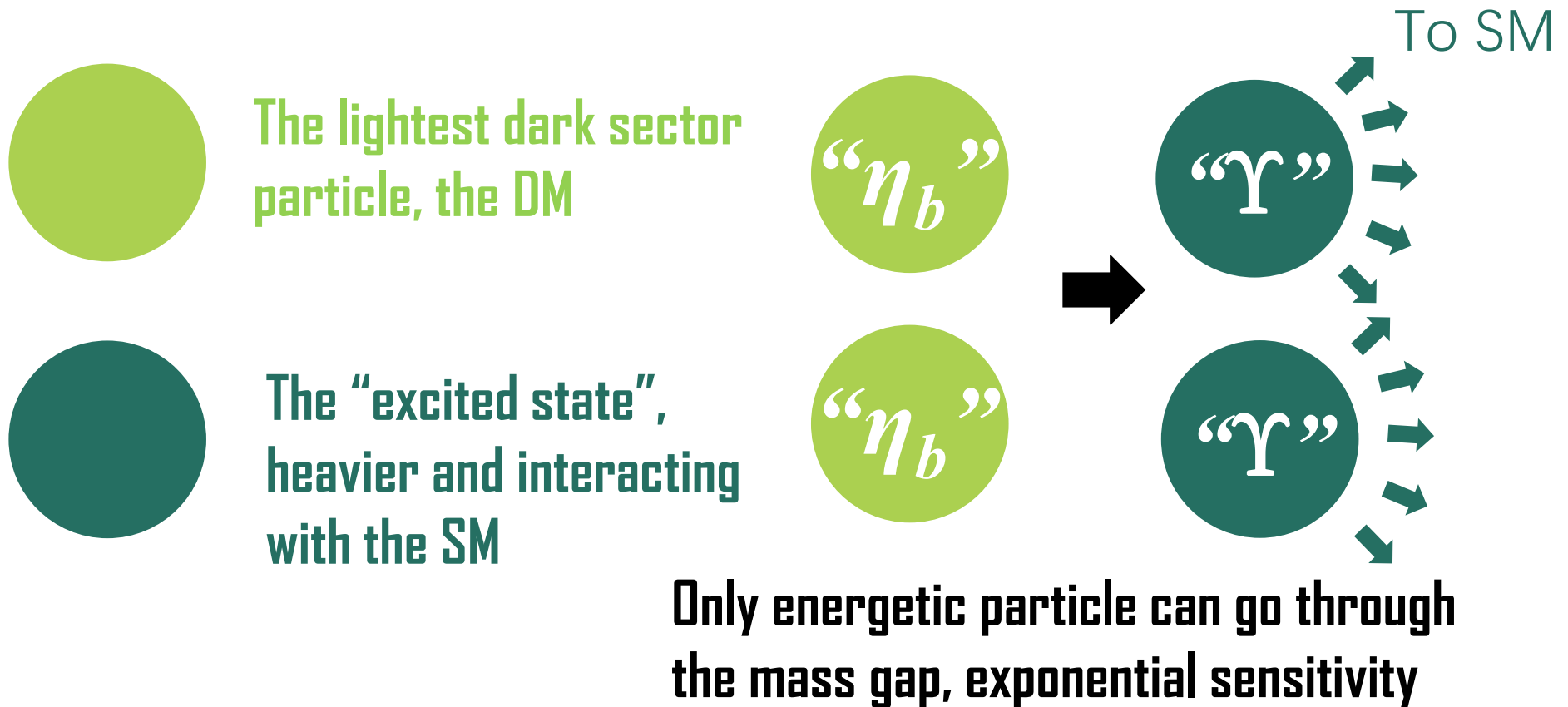
2604.06315 H-C. Cheng, X. Jiang, LFL, E. Salvioni

+2408.13304 H-C. Cheng, X. Jiang, LFL

+2401.08785 H-C. Cheng, X. Jiang, LFL, E. Salvioni

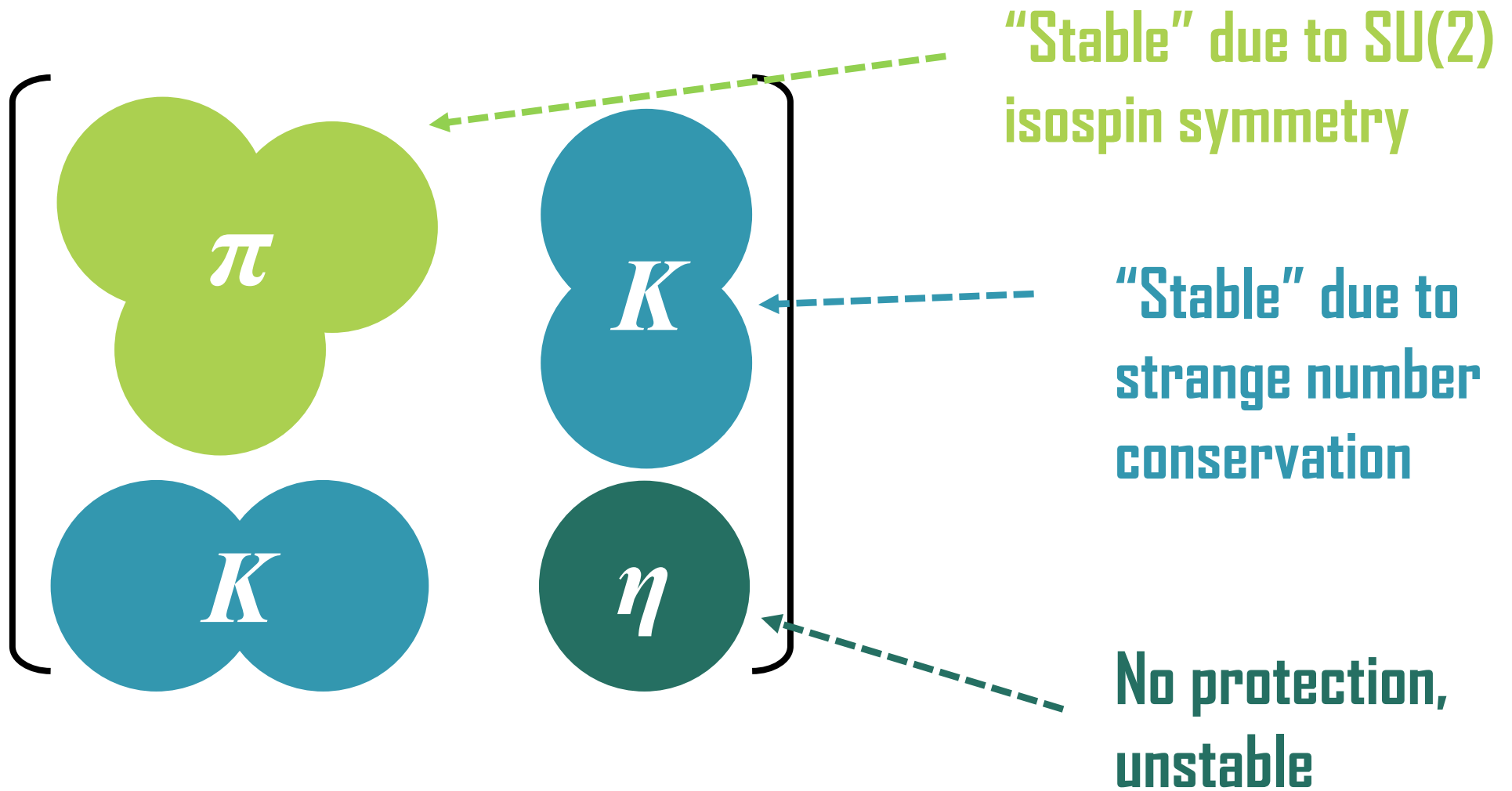
+2110.10691 H-C. Cheng, LFL, E. Salvioni

Forbidden Composite DM



R.T. D'Agnolo and J.T. Ruderman, 1505.07107; LFL, Y. Tsai, 1901.0993;
E. Bernreuther, F. Kahlhoefer, M. Kramer and P. Tunney, 1907.04346.....

Back in the SM



Possible Thermal Mechanisms



The messenger: heavy meson that decays, contact with the SM



The DM meson, non-interacting



The intermediate, exists in many models

Y. Hochberg, E.
Kuflik, H. Murayama,
T. Volansky, J.
Wacker, 1411.3727;
A. Katz, E.
Salvioni, and B.
Shakya, 2006.15148.....



SIMP-like



Pairwise



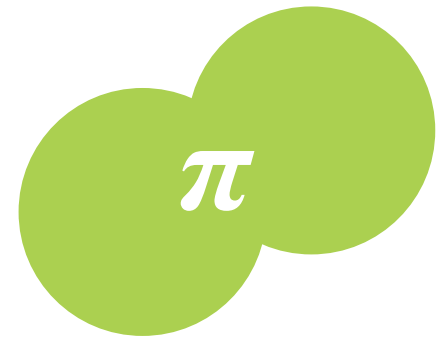
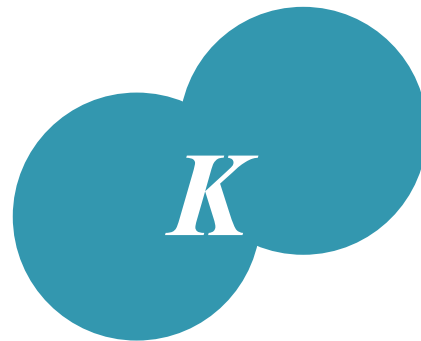
Scattering

The (Minimal) Model

Gauge group: $SO(N_c) \quad N_c \geq 4$

$SU(3)/SO(3) \Rightarrow$ 5 Goldstone bosons

Two π , two K and one η



$$m_\eta = (1 + \Delta_\eta) m_\pi > m_K = (1 + \Delta_K) m_\pi > m_\pi$$

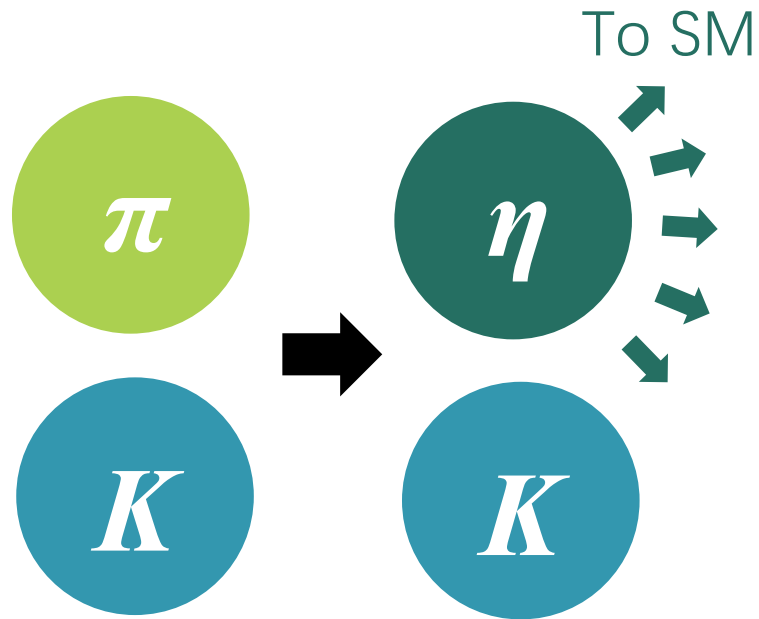
$$\hat{\eta}_0 = \hat{\pi}_8 \quad \hat{K}_{\pm 1/2} = \frac{1}{\sqrt{2}}(\hat{\pi}_4 \mp i\hat{\pi}_6) \quad \hat{\pi}_\pm = \frac{1}{\sqrt{2}}(\hat{\pi}_3 \mp i\hat{\pi}_1)$$

Leading ChPT Lagrangian (Low Temp)

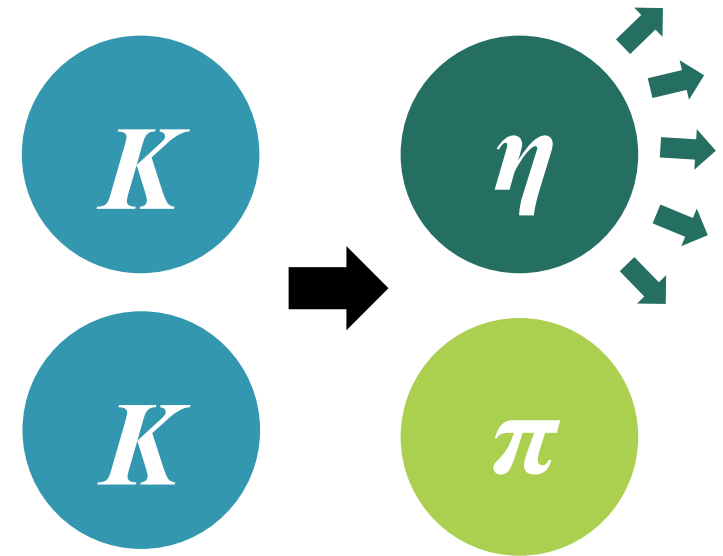
$$\begin{aligned}
\mathcal{L}_2 \supset & \frac{1}{24f^2} \left\{ m_{\hat{\pi}}^2 \left[\hat{\eta}_0^2 + 2\hat{\pi}_+\hat{\pi}_- + 2\hat{K}_{+1/2}\hat{K}_{-1/2} \right]^2 + 2(m_{\hat{K}}^2 - m_{\hat{\pi}}^2) \left[\frac{8}{9}\hat{\eta}_0^4 + 3\hat{\eta}_0^2\hat{K}_{+1/2}\hat{K}_{-1/2} \right. \right. \\
& \left. \left. - \sqrt{\frac{2}{3}}(\hat{\eta}_0\hat{K}_{+1/2}^2\hat{\pi}_- + \hat{\eta}_0\hat{K}_{-1/2}^2\hat{\pi}_+) + 2\hat{K}_{+1/2}^2\hat{K}_{-1/2}^2 + 2\hat{K}_{+1/2}\hat{K}_{-1/2}\hat{\pi}_+\hat{\pi}_- \right] \right\} \\
& + \frac{1}{24f^2} \left\{ 4(\partial\hat{\pi}_+)^2\hat{\pi}_-^2 + 4\hat{\pi}_+^2(\partial\hat{\pi}_-)^2 - 8\partial\hat{\pi}_+\hat{\pi}_+\partial\hat{\pi}_-\hat{\pi}_- + (\partial\hat{K}_{+1/2})^2\hat{K}_{-1/2}^2 + \hat{K}_{+1/2}^2(\partial\hat{K}_{-1/2})^2 \right. \\
& - 2\partial\hat{K}_{+1/2}\hat{K}_{+1/2}\partial\hat{K}_{-1/2}\hat{K}_{-1/2} + 8\hat{K}_{+1/2}\partial\hat{K}_{-1/2}\hat{\pi}_+\partial\hat{\pi}_- + 8\partial\hat{K}_{+1/2}\hat{K}_{-1/2}\partial\hat{\pi}_+\hat{\pi}_- \\
& - 4\hat{K}_{+1/2}\hat{K}_{-1/2}\partial\hat{\pi}_+\partial\hat{\pi}_- - 4\hat{K}_{+1/2}\partial\hat{K}_{-1/2}\partial\hat{\pi}_+\hat{\pi}_- - 4\partial\hat{K}_{+1/2}\hat{K}_{-1/2}\hat{\pi}_+\partial\hat{\pi}_- \\
& - 4\partial\hat{K}_{+1/2}\partial\hat{K}_{-1/2}\hat{\pi}_+\hat{\pi}_- - 6\hat{\eta}_0^2\partial\hat{K}_{+1/2}\partial\hat{K}_{-1/2} - 6(\partial\hat{\eta}_0)^2\hat{K}_{+1/2}\hat{K}_{-1/2} \\
& + 6\hat{\eta}_0\partial\hat{\eta}_0\partial\hat{K}_{+1/2}\hat{K}_{-1/2} + 6\hat{\eta}_0\partial\hat{\eta}_0\hat{K}_{+1/2}\partial\hat{K}_{-1/2} + 2\sqrt{6} \left[\partial\hat{\eta}_0\partial\hat{K}_{-1/2}\hat{K}_{-1/2}\hat{\pi}_+ \right. \\
& + \partial\hat{\eta}_0\partial\hat{K}_{+1/2}\hat{K}_{+1/2}\hat{\pi}_- - \partial\hat{\eta}_0\hat{K}_{+1/2}^2\partial\hat{\pi}_- - \partial\hat{\eta}_0\hat{K}_{-1/2}^2\partial\hat{\pi}_+ - \hat{\eta}_0(\partial\hat{K}_{-1/2})^2\hat{\pi}_+ \\
& \left. \left. - \hat{\eta}_0(\partial\hat{K}_{+1/2})^2\hat{\pi}_- + \hat{\eta}_0\partial\hat{K}_{-1/2}\hat{K}_{-1/2}\partial\hat{\pi}_+ + \hat{\eta}_0\partial\hat{K}_{+1/2}\hat{K}_{+1/2}\partial\hat{\pi}_- \right] \right\}. \tag{A.1}
\end{aligned}$$

**Mass & 4-point
interaction terms**

Important Alternative Processes



K assisted conversion, low Boltzmann suppression



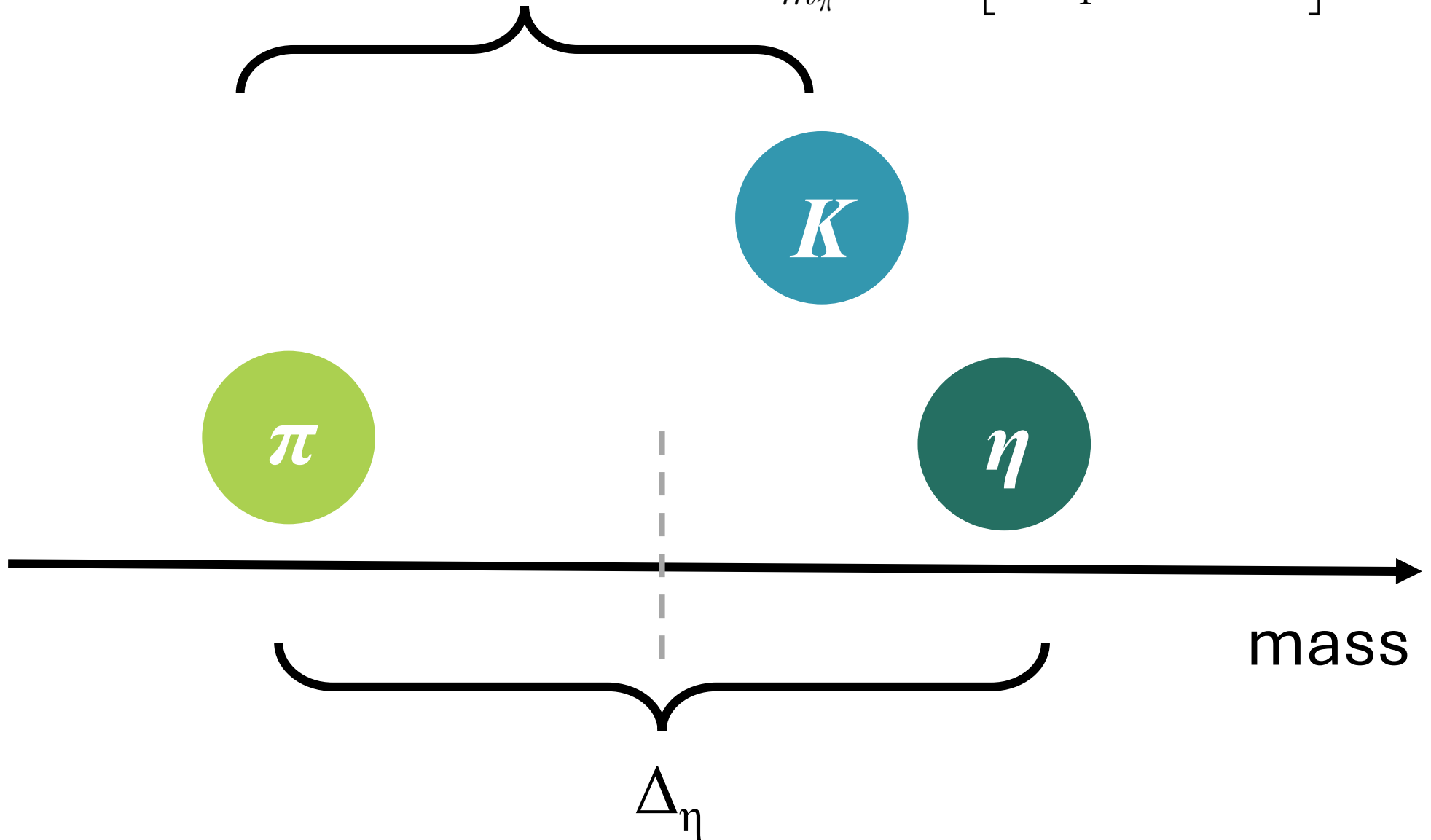
K annihilation, gives indirect detection signals

The key scattering terms

$$\begin{aligned} \frac{dY_{\hat{\pi}}}{dx} = & -\frac{s(x)}{\tilde{H}(x)x} \left[-\langle \sigma v \rangle_{\hat{K}\hat{K} \rightarrow \hat{\pi}\hat{\pi}} \left(Y_{\hat{K}}^2 - Y_{\hat{K}}^{\text{eq}2} \frac{Y_{\hat{\pi}}^2}{Y_{\hat{\pi}}^{\text{eq}2}} \right) - \frac{1}{2} \langle \sigma v \rangle_{\hat{K}\hat{K} \rightarrow \hat{\pi}\hat{\eta}} \left(Y_{\hat{K}}^2 - Y_{\hat{K}}^{\text{eq}2} \frac{Y_{\hat{\pi}}Y_{\hat{\eta}}}{Y_{\hat{\pi}}^{\text{eq}}Y_{\hat{\eta}}^{\text{eq}}} \right) \right. \\ & \left. - \langle \sigma v \rangle_{\hat{K}\hat{\eta} \rightarrow \hat{K}\hat{\pi}} \left(Y_{\hat{K}}Y_{\hat{\eta}} - Y_{\hat{\eta}}^{\text{eq}} \frac{Y_{\hat{K}}Y_{\hat{\pi}}}{Y_{\hat{\pi}}^{\text{eq}}} \right) - \frac{1}{2} \langle \sigma v \rangle_{\hat{\eta}\hat{\eta} \rightarrow \hat{\pi}\hat{\pi}} \left(Y_{\hat{\eta}}^2 - Y_{\hat{\eta}}^{\text{eq}2} \frac{Y_{\hat{\pi}}^2}{Y_{\hat{\pi}}^{\text{eq}2}} \right) \right] \\ & - \frac{s(x)^2}{\tilde{H}(x)x} \left[2 \langle \sigma v^2 \rangle_{\hat{K}\hat{\pi}\hat{\pi} \rightarrow \hat{\eta}\hat{K}} \left(Y_{\hat{K}}Y_{\hat{\pi}}^2 - Y_{\hat{\pi}}^{\text{eq}2} \frac{Y_{\hat{\eta}}Y_{\hat{K}}}{Y_{\hat{\eta}}^{\text{eq}}} \right) + \langle \sigma v^2 \rangle_{\hat{\eta}\hat{\pi}\hat{\pi} \rightarrow \hat{K}\hat{K}} \left(Y_{\hat{\eta}}Y_{\hat{\pi}}^2 - Y_{\hat{\eta}}^{\text{eq}}Y_{\hat{\pi}}^{\text{eq}2} \frac{Y_{\hat{K}}^2}{Y_{\hat{K}}^{\text{eq}2}} \right) \right. \\ & \left. - \langle \sigma v^2 \rangle_{\hat{\eta}\hat{K}\hat{K} \rightarrow \hat{\pi}\hat{\pi}} \left(Y_{\hat{\eta}}Y_{\hat{K}}^2 - Y_{\hat{\eta}}^{\text{eq}}Y_{\hat{K}}^{\text{eq}2} \frac{Y_{\hat{\pi}}^2}{Y_{\hat{\pi}}^{\text{eq}2}} \right) \right], \quad (\text{A.9}) \end{aligned}$$

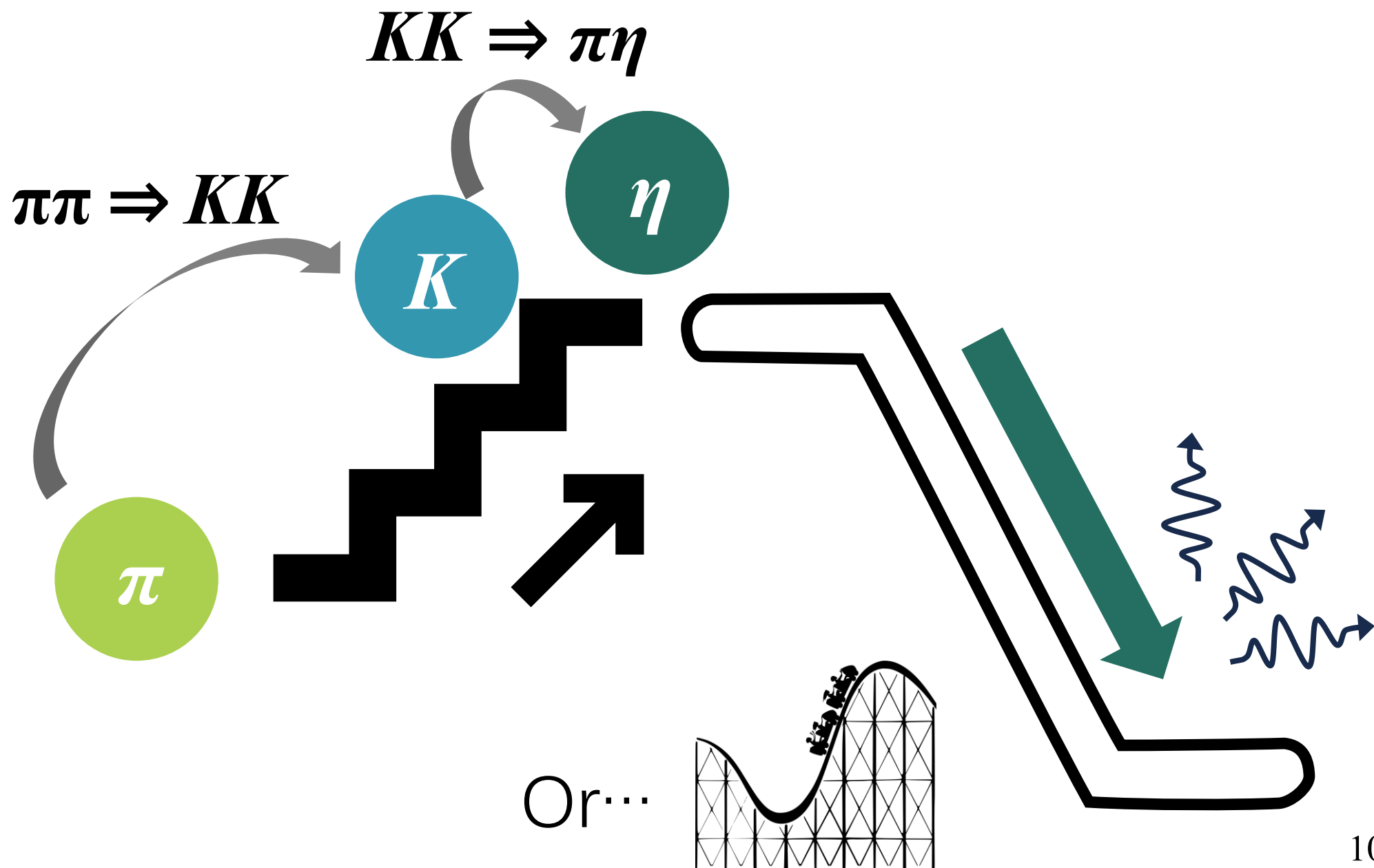
5-pt WZW terms negligible

$$\Delta_K \quad \Delta_{\hat{K}} \equiv \frac{m_{\hat{K}}}{m_{\hat{\pi}}} - 1 = \left[1 + \frac{3}{4} \Delta_{\hat{\eta}} (2 + \Delta_{\hat{\eta}}) \right]^{1/2} - 1$$

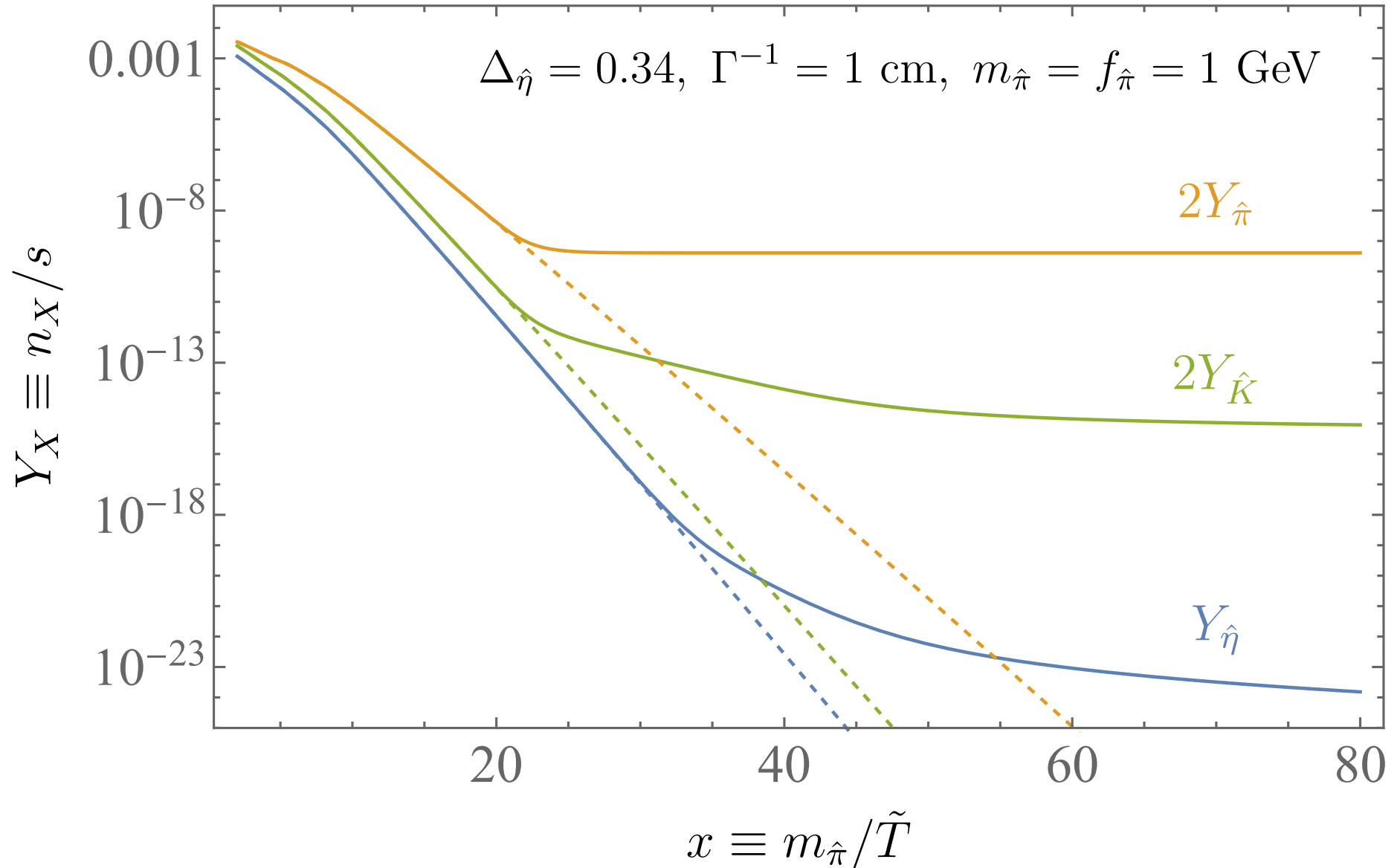


$KK \Rightarrow \pi\eta$ onshell and unsuppressed

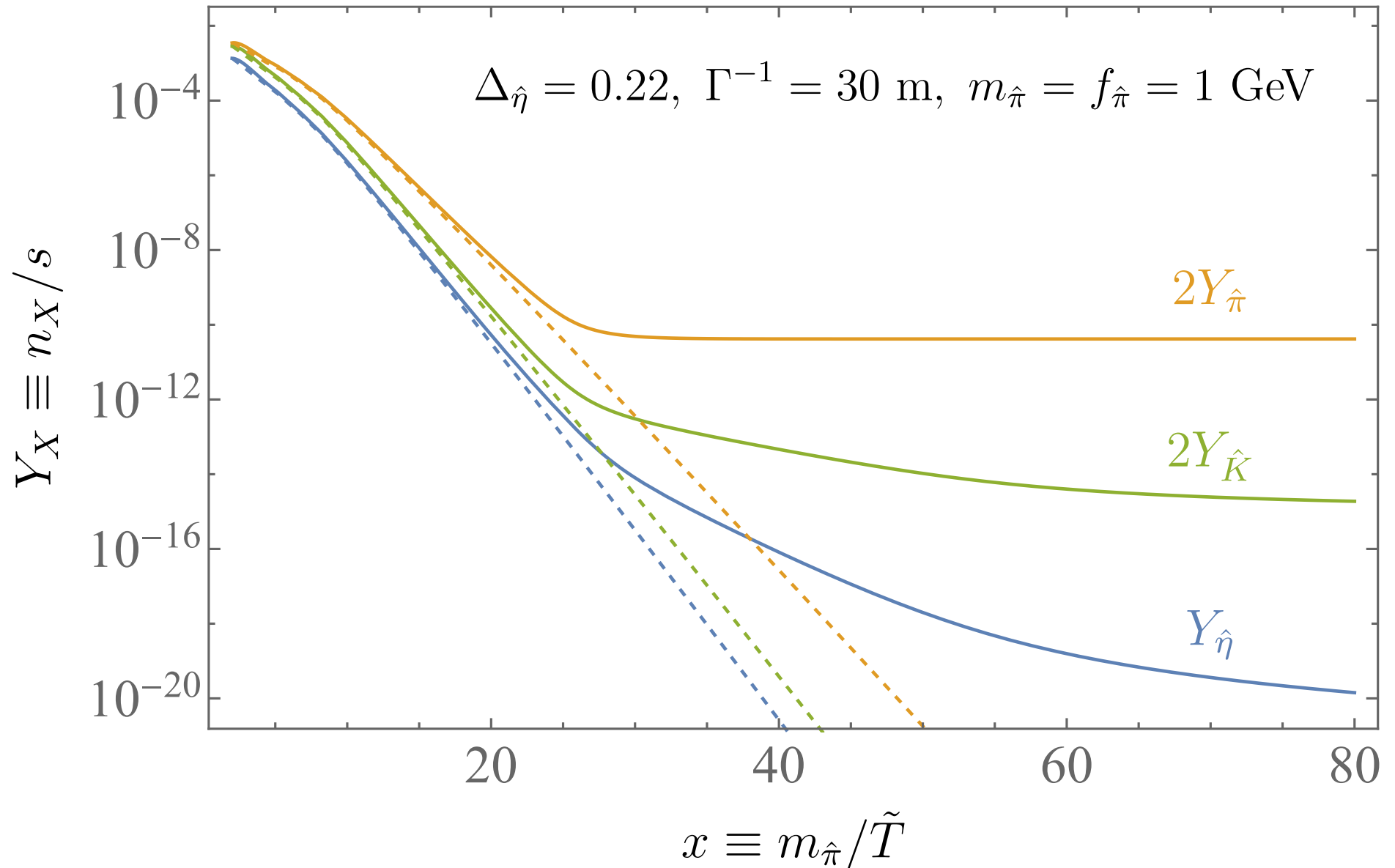
The “Sliding” Process



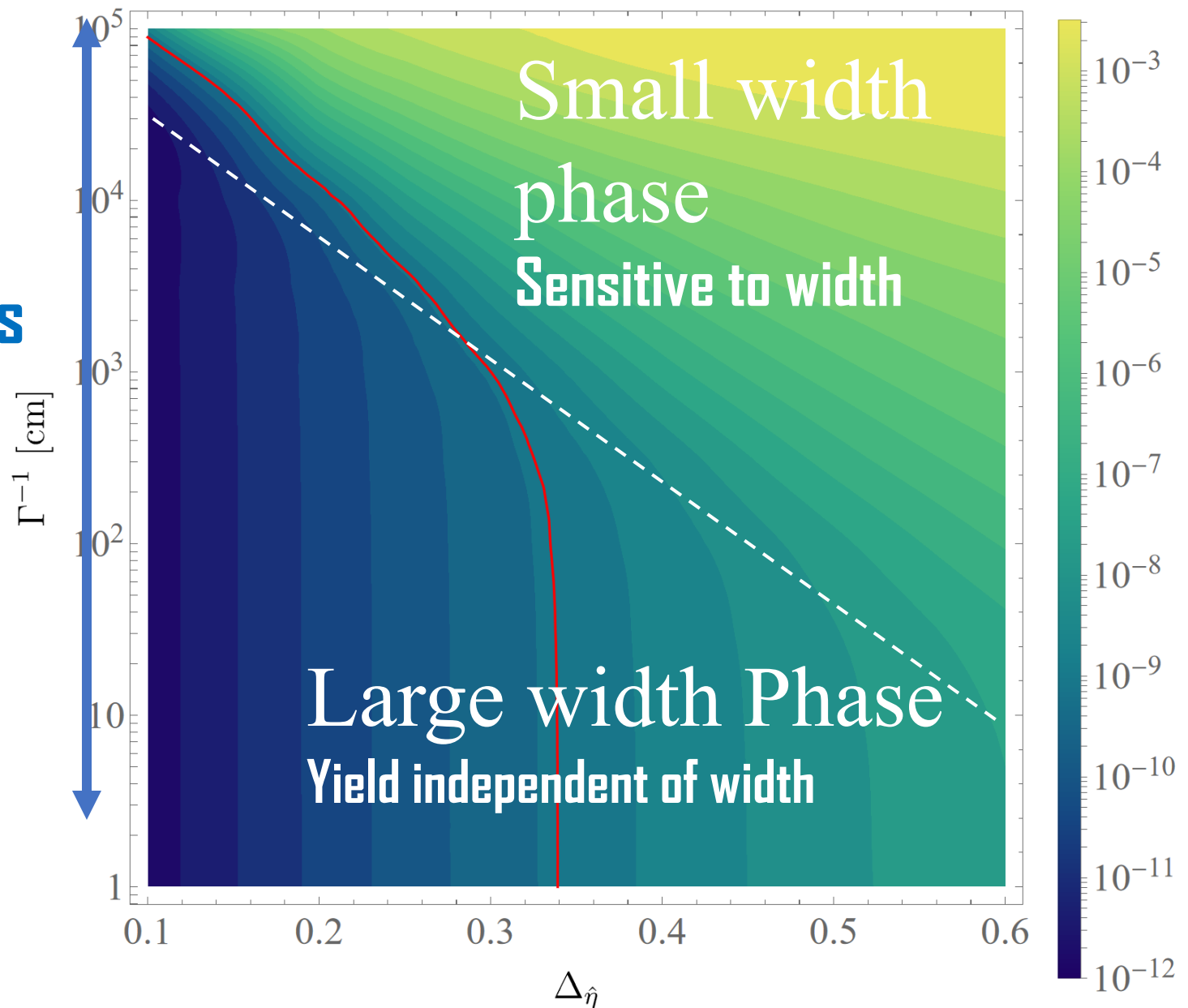
Large Decay Width Limit: Freezeout Controlled by Conversion

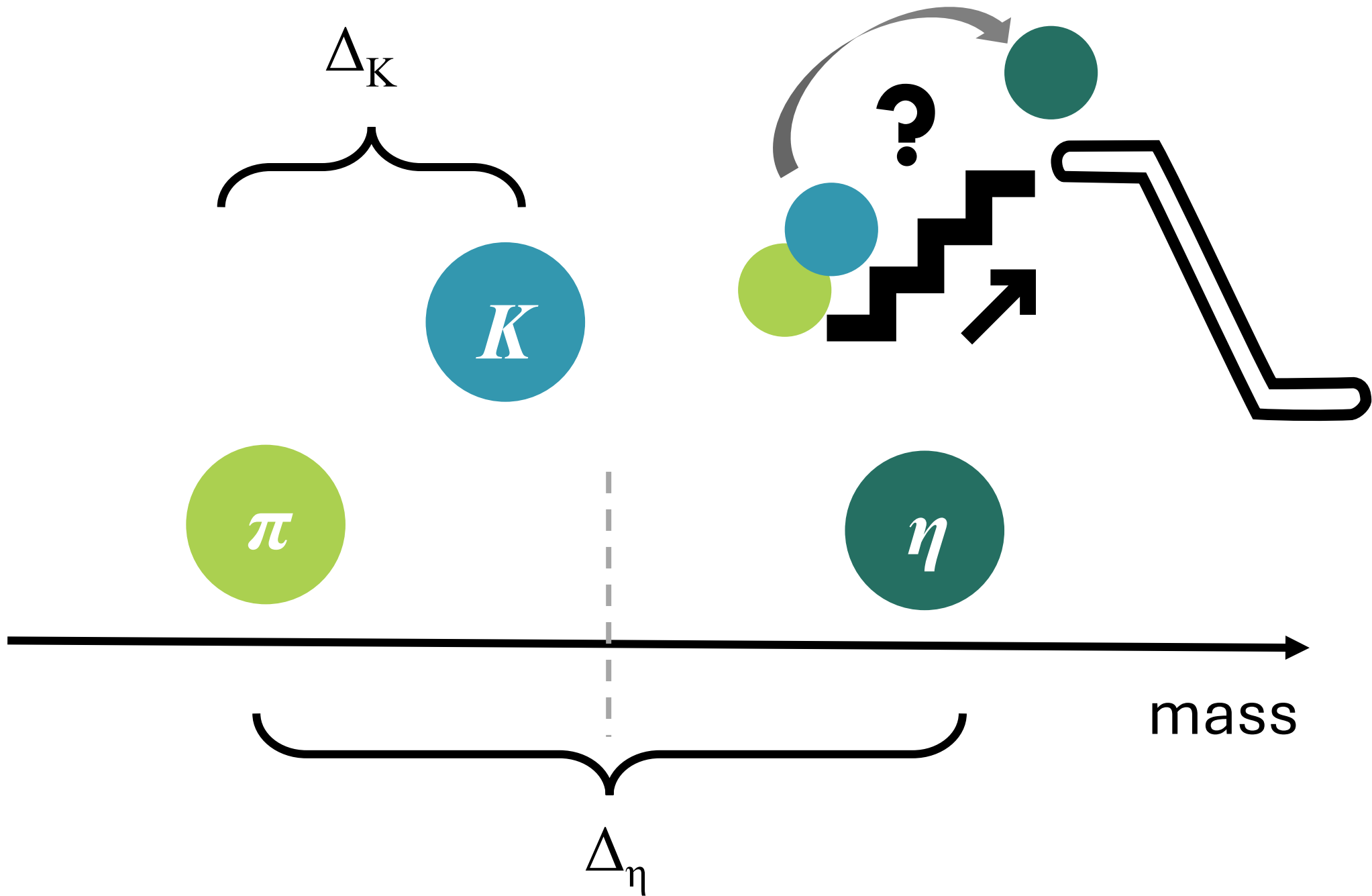


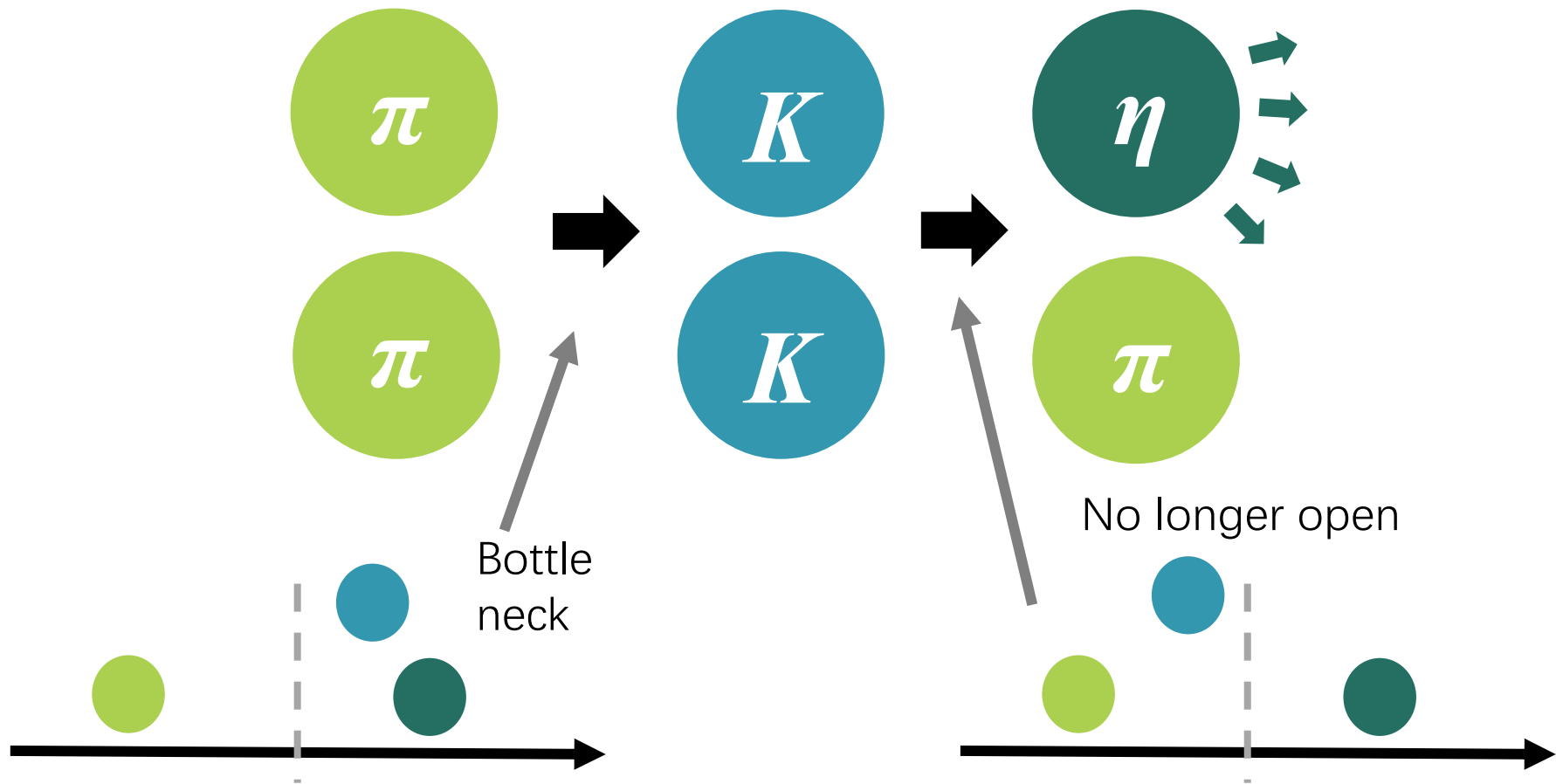
Small Decay Width Limit: Freezeout Controlled by Decay



Decay at Human/Lab Length Scales

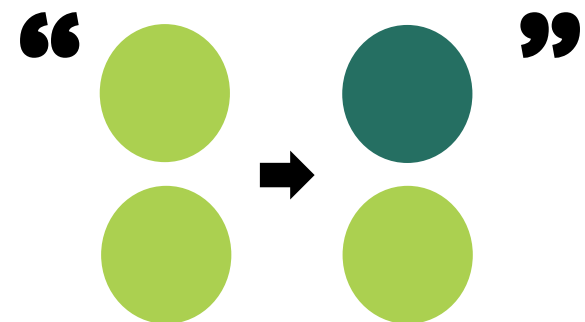
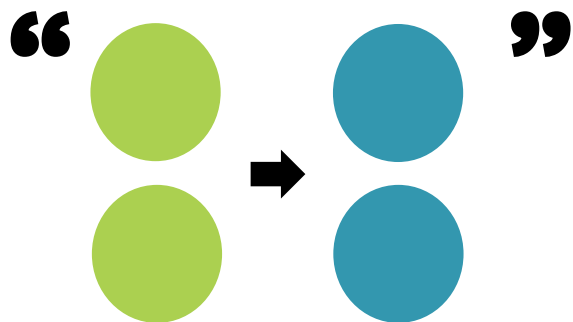






Effectively $\pi\pi \Rightarrow KK$

Effectively $\pi\pi \Rightarrow \pi\eta$

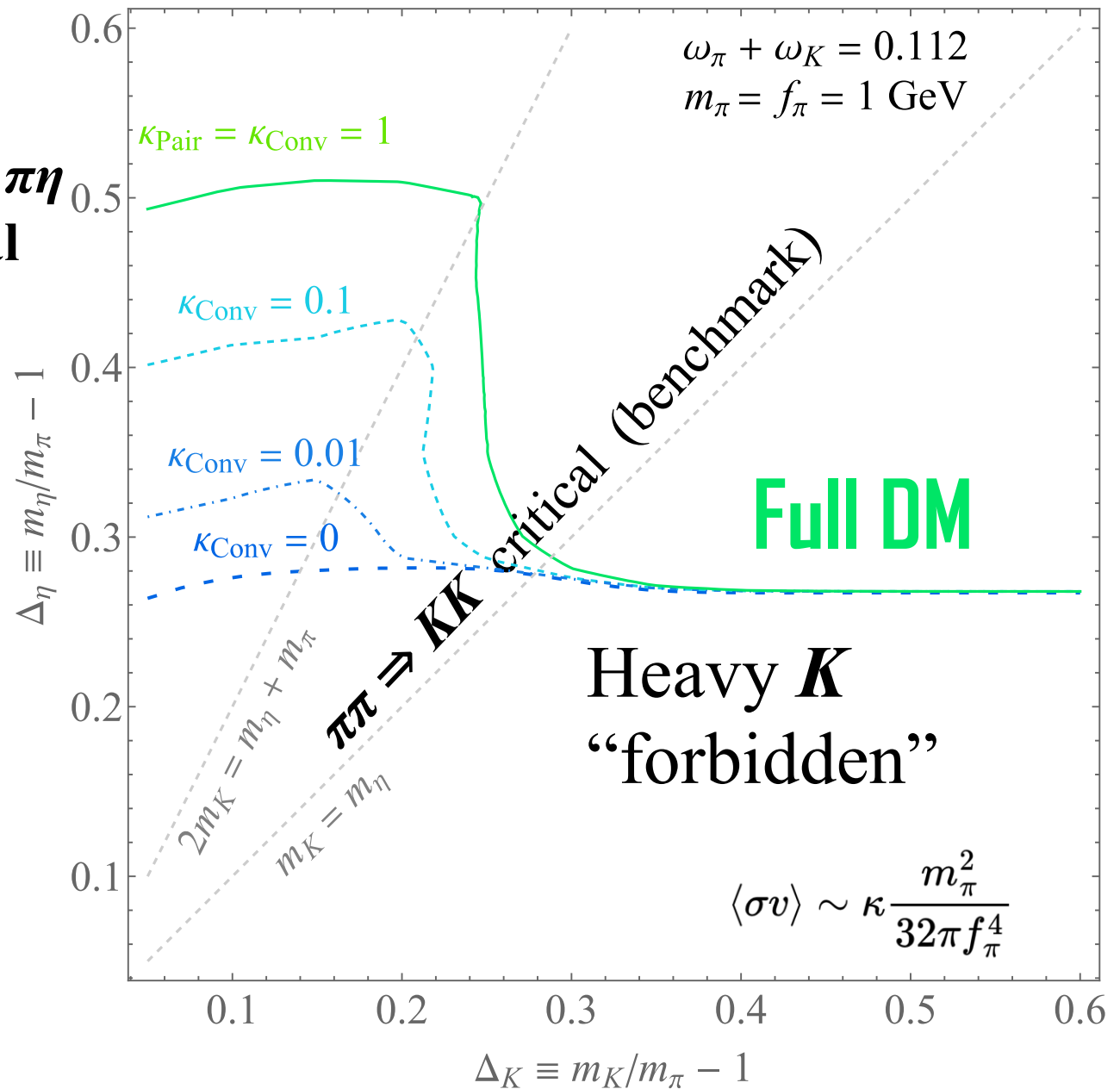


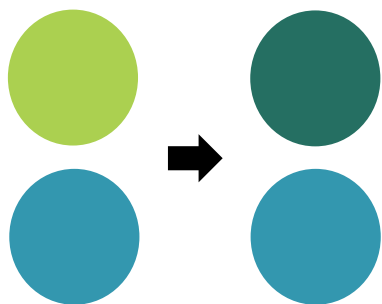
Extended Phases

At least 3 extra dynamic phases recognized

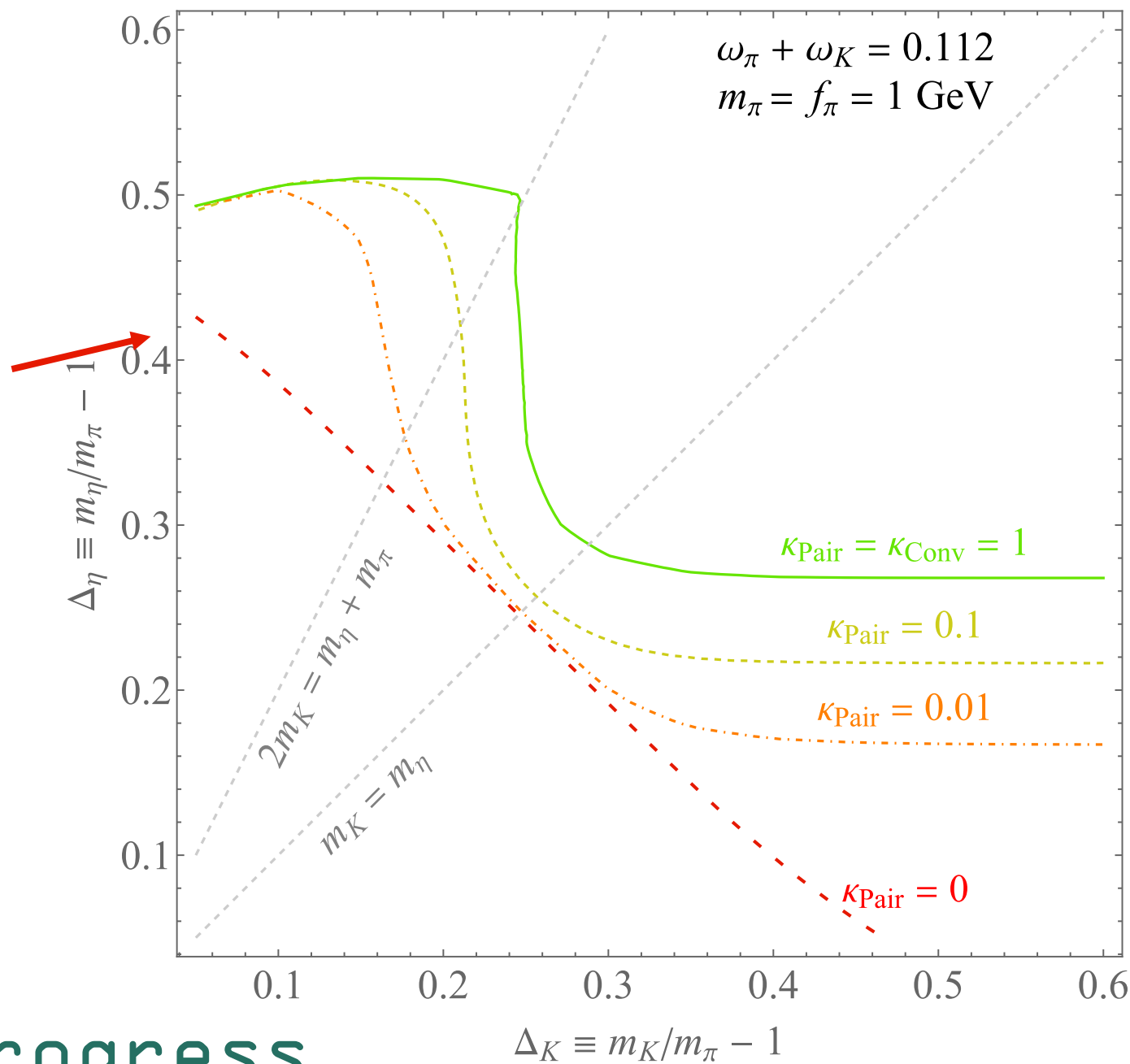
$KK \Rightarrow \pi\eta$
critical

* Assuming all processes having similar cross sections, not necessarily true for realistic models

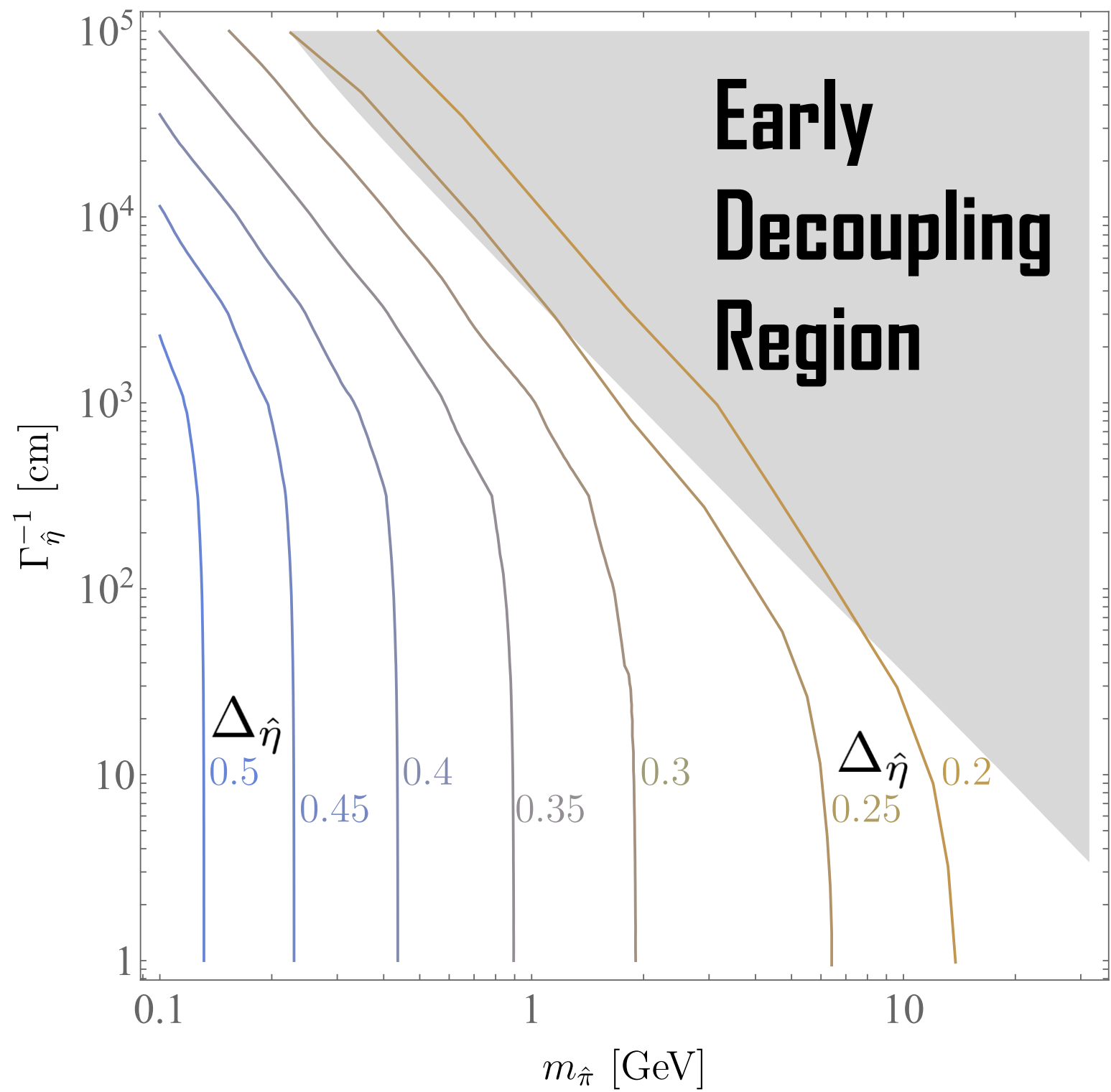




Full $\pi K \rightarrow \eta K$
dominance



Work in progress



Direct Detection Prospects

The leading Z exchange between DM and SM are forbidden by the same parity that stabilizes the DM

$$\psi_i \xrightarrow{\mathcal{C}} -(-1)^i \psi_i$$

$$\Rightarrow \hat{\pi}_{\pm} \rightarrow \hat{\pi}_{\mp}$$

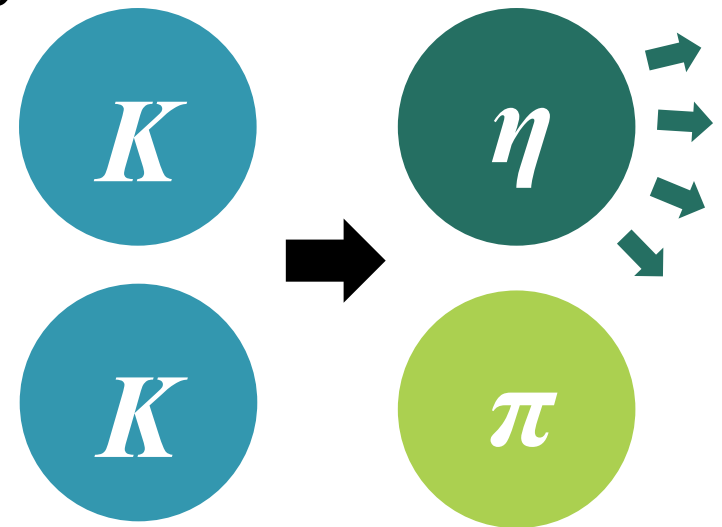
The leading vector portal scattering is forbidden:

~~$$i(\hat{\pi}_+ \partial_{\mu} \hat{\pi}_- - \hat{\pi}_- \partial_{\mu} \hat{\pi}_+) J_{\text{SM}}^{\mu}$$~~

Higgs/scalar portal interaction is still possible.....

Indirect Detection Prospects

- As forbidden dark matter, usually free from indirect detection
- The remaining secondary Kaon DM can annihilate to SM, strongly depending on how many K remain



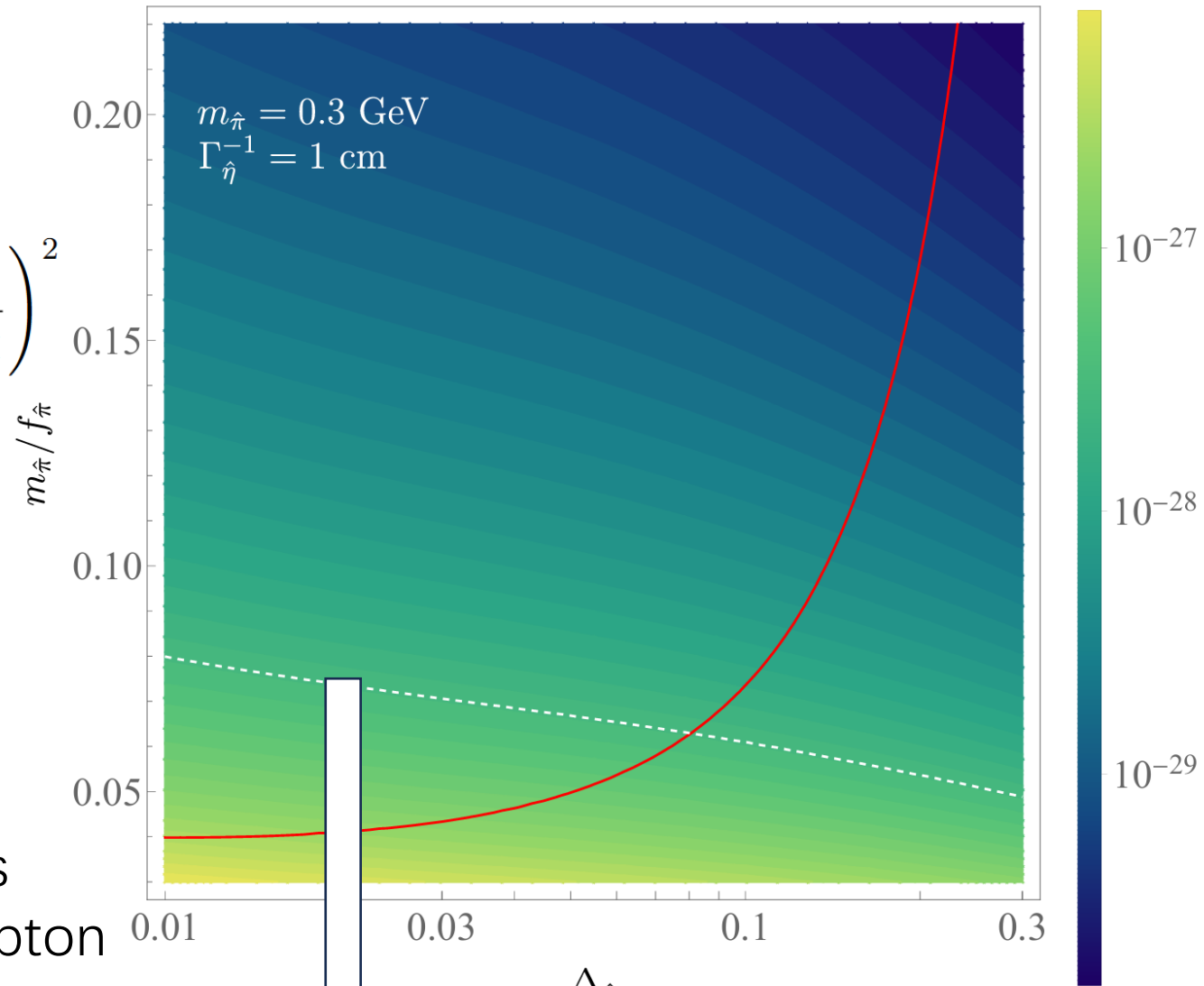
The most stringent CMB spectral distortion limit constraints the highly degenerate case (Δ of a few %)

Effective Annihilation Xsec

$$\langle\sigma v\rangle_{\text{eff}} \equiv \frac{\xi^2}{2} \langle\sigma v\rangle_{\hat{K}\hat{K}\rightarrow\hat{\pi}\hat{\eta}} \left(\frac{2Y_{\hat{K}}^0 m_{\hat{K}}}{Y_{\text{DM}} m_{\text{DM}}} \right)^2$$

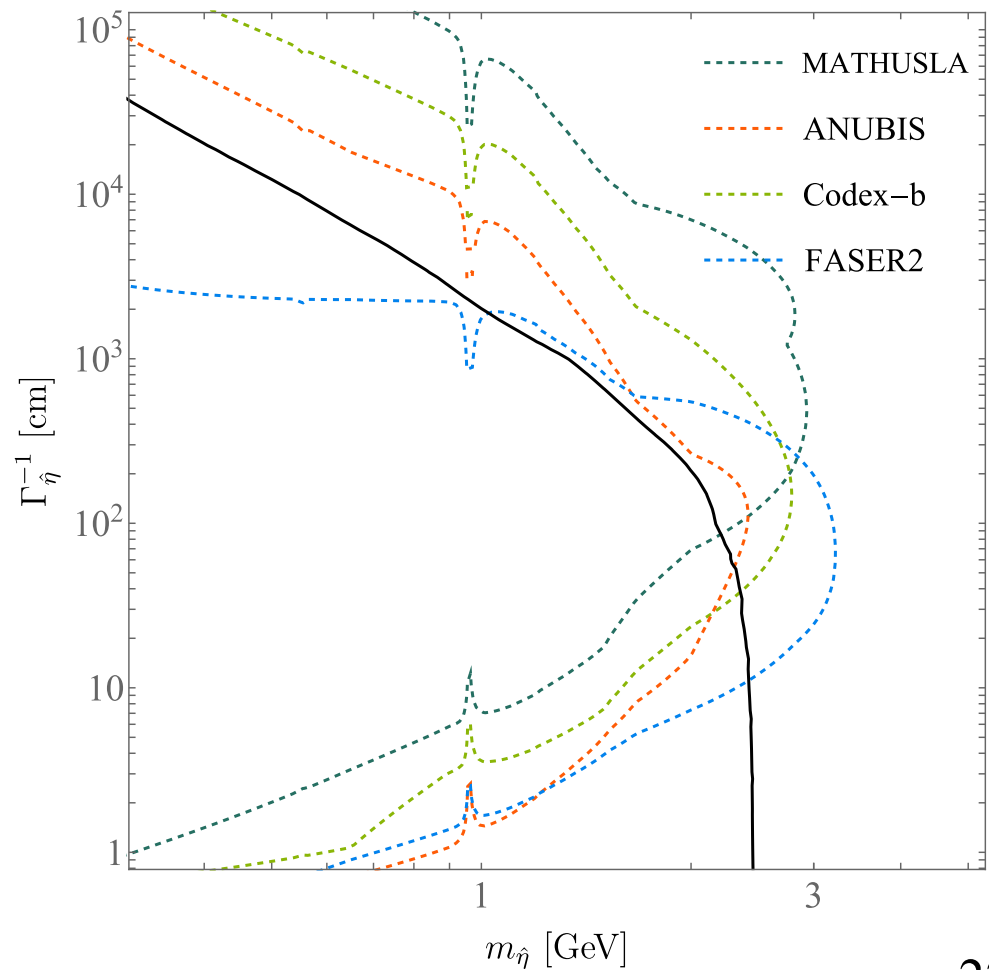
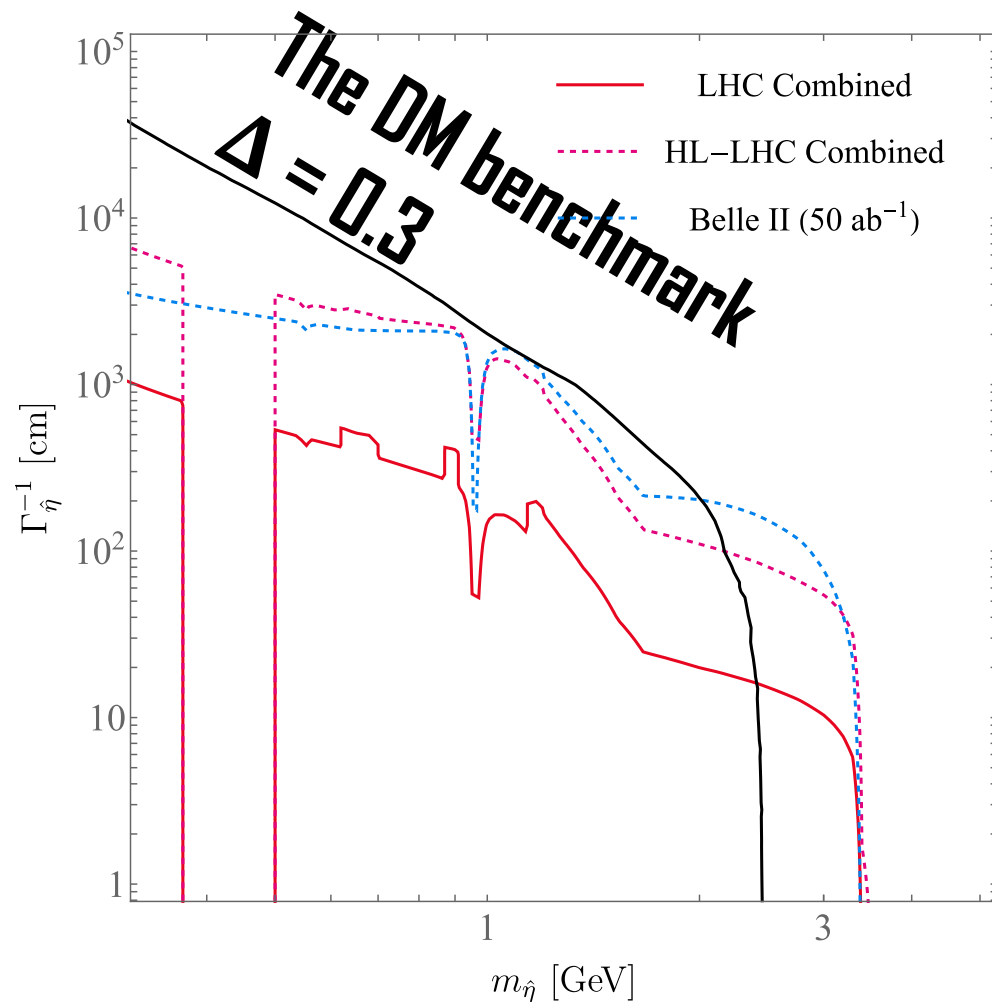
Signals include:

- ☐ Primary gamma photons
- ☐ Secondary inverse-Compton photons
- ☐ Cosmic ray
- ☐ CMB spectral distortions



$\Delta_{\hat{\eta}}$
**Too much K
annihilation**

Collider Bounds When η Decays to Muons (Model Dependent)



Future Prospects?

- ☐ Freeze out $\Rightarrow$ Freeze in
- ☐ Collider $\Rightarrow$ Beam Dumps
- ☐ Better Direct/Indirect predictions
- ☐