

# 利用数值方法研究宇宙线在不同时间尺度上的太阳调制

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3 Center for Space Research, North-West University

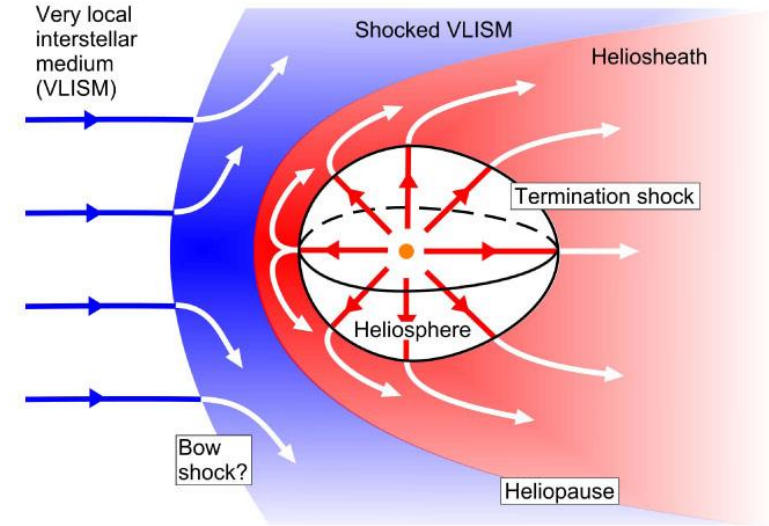
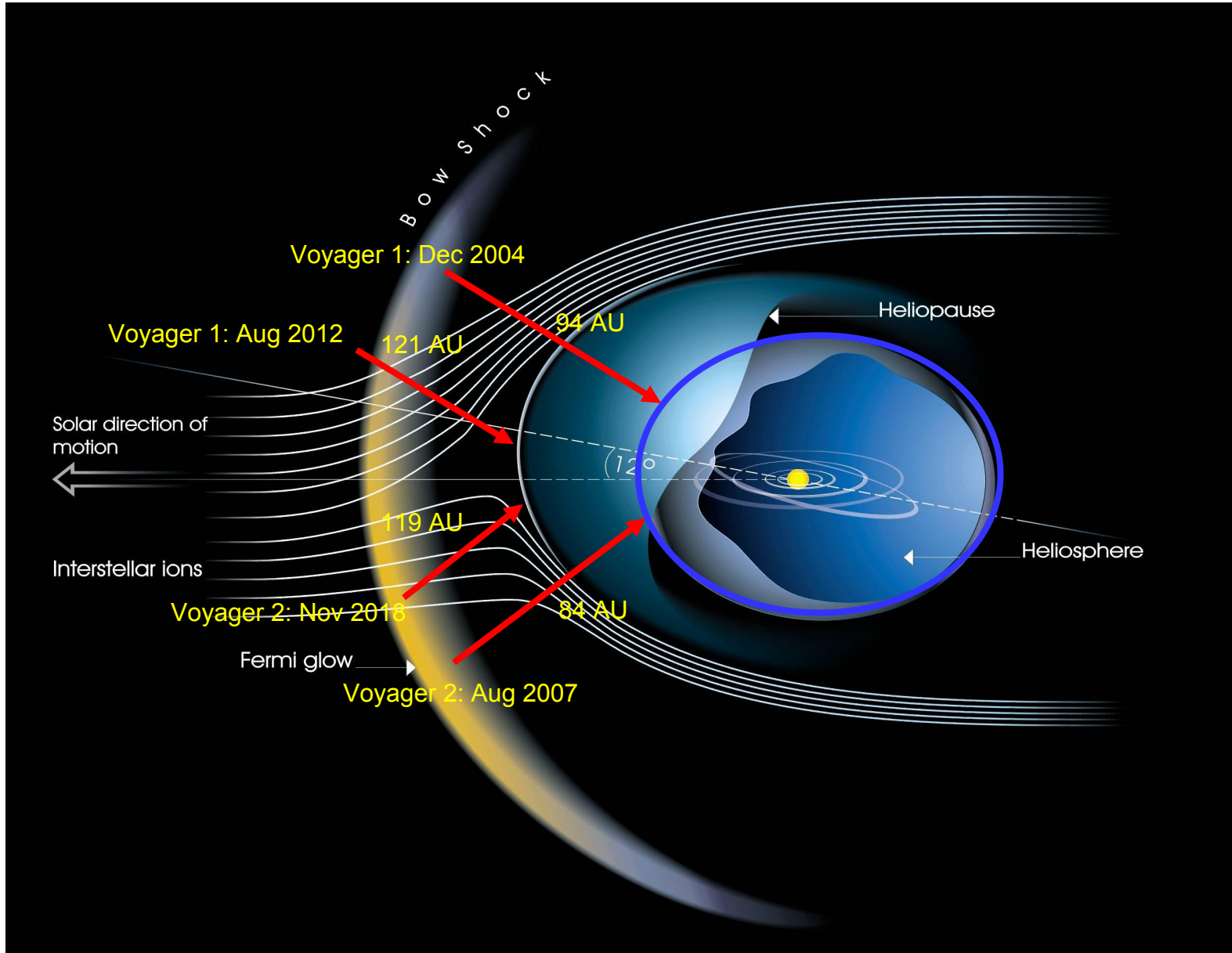
4 Florida Institute of Technology

# Outline

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- **The Solar Wind, Heliosphere**
- **Modulation Theory, Numerical Model**
- **Long-term Modulation**
- **Short-term Modulation**

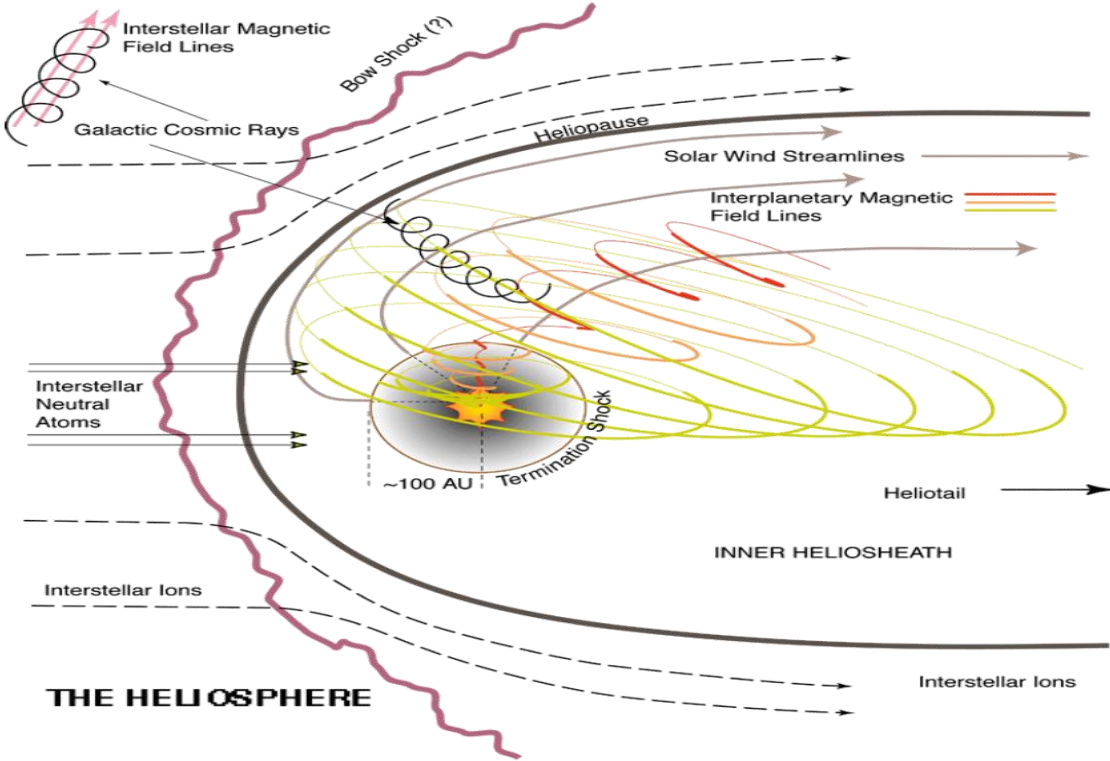
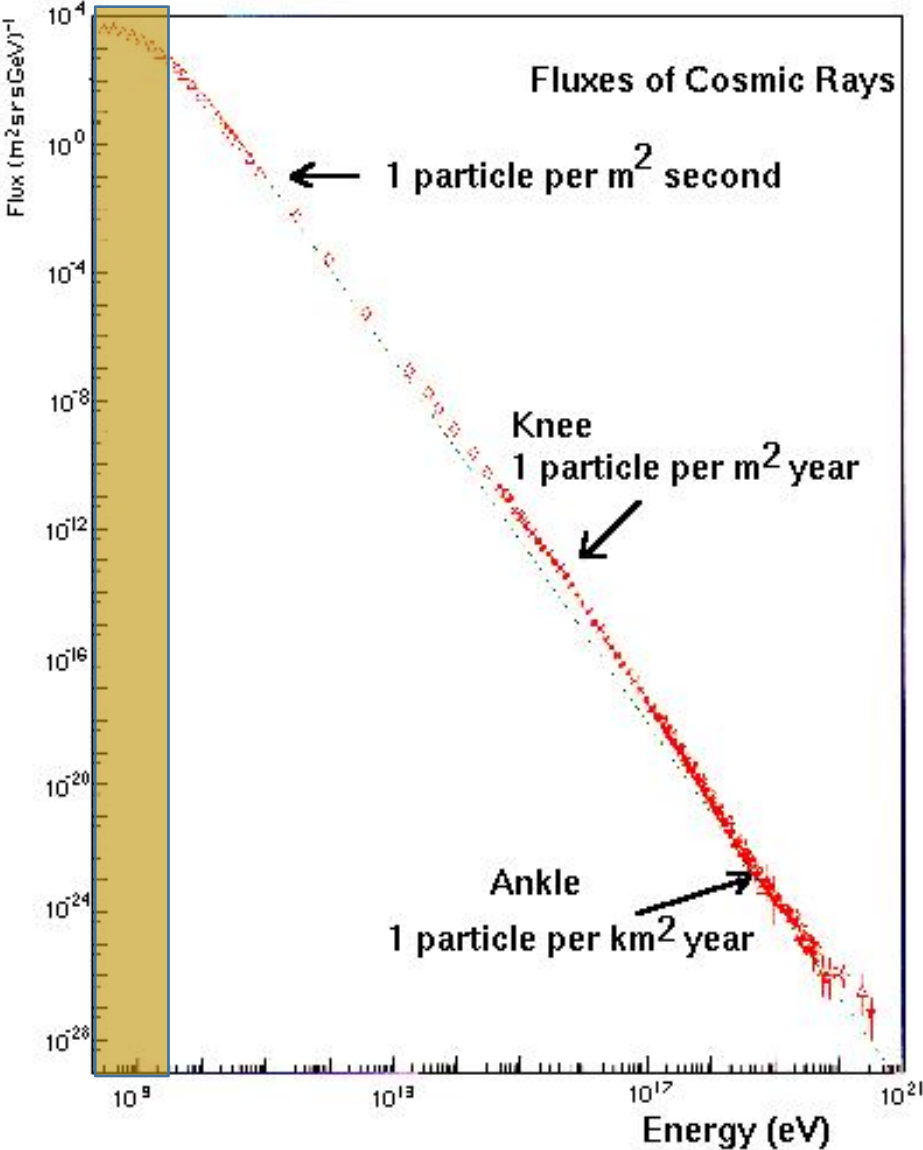
# Heliosphere



Owens and Forsyth. Living Rev. 2013

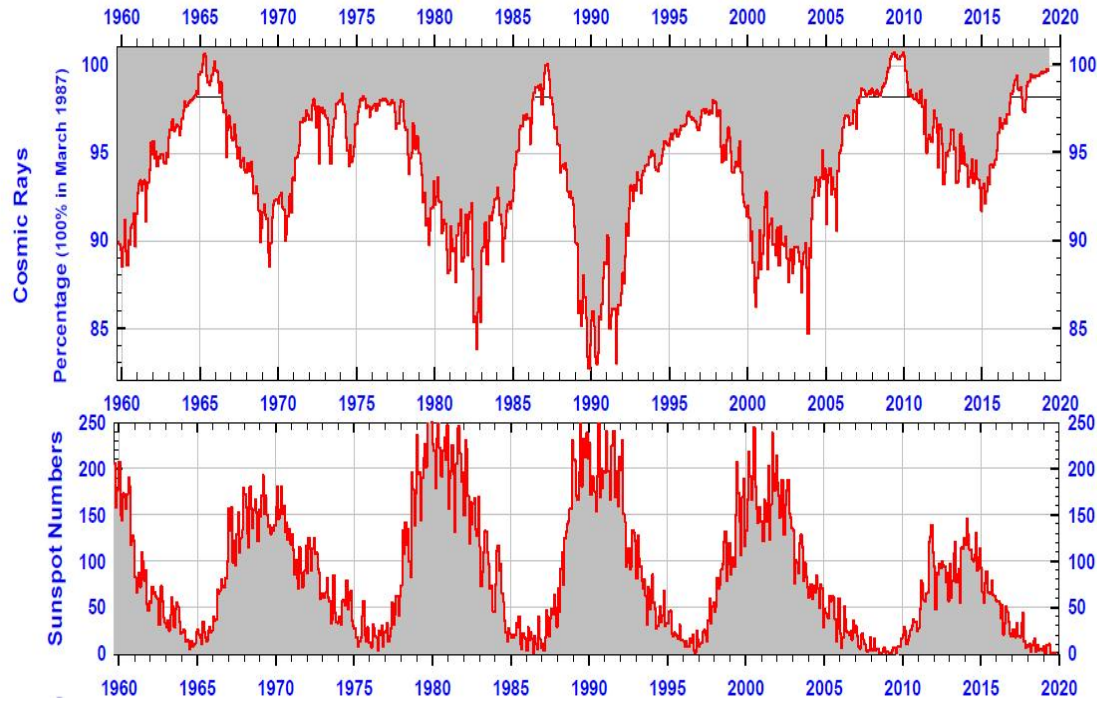
**1 au Solar Wind:**  
400 km/s  
mainly protons and electrons  
 $\sim 6 \text{ cm}^{-3}$   
 $10^5 \text{ K}$

# Galactic Cosmic Ray Spectrum for Solar Modulation



Cosmic ray Protons with energy below about  $\sim 30$  GeV are subject to solar modulation

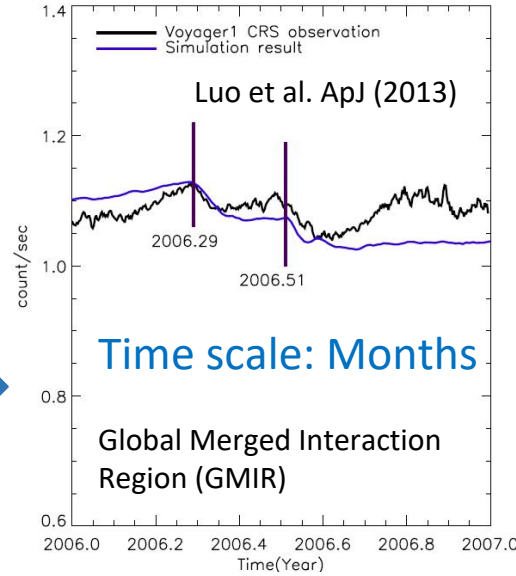
# GCR Solar Modulation



Time scale: Years

Potgieter, LRSP(2013)

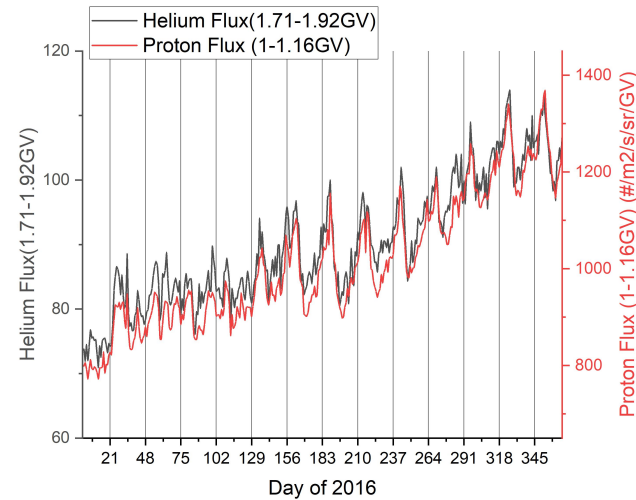
Galactic Cosmic Rays (GCR) is modulated by the Sun at different time scales, which are related to different solar activities and solar wind structures.



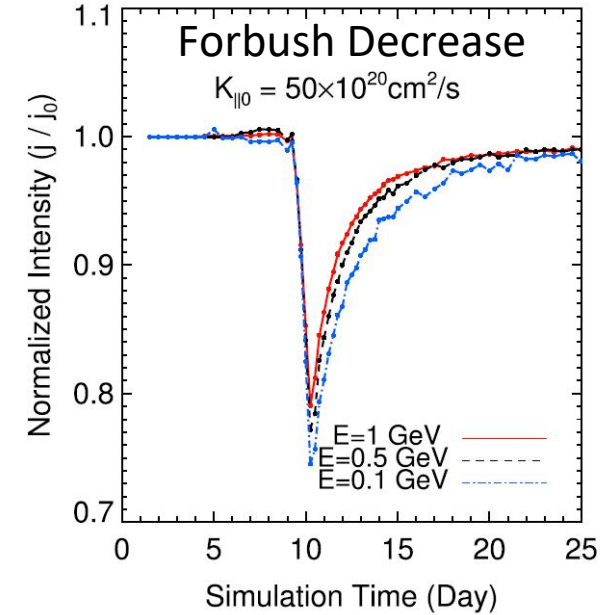
Luo et al. ApJ (2013)

Time scale: Months

Global Merged Interaction Region (GMIR)



Luo et al. ApJ (2017)



Time scale: Days

# GCR Transport Theory

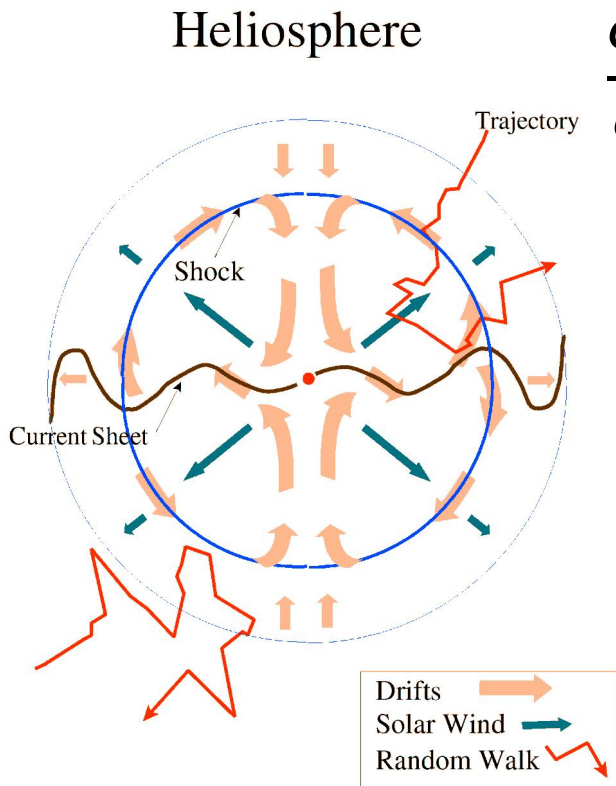
Convection **Drift**

Diffusion

Adiabatic Energy Change

$$\frac{\partial f}{\partial t} = - (V_{sw} + \langle V_d \rangle) \cdot \nabla f + \nabla \cdot (K_s \cdot \nabla f) + \frac{1}{3} (\nabla \cdot V_{sw}) \frac{\partial f}{\partial \ln p} \quad (E. N. Parker 1965)$$

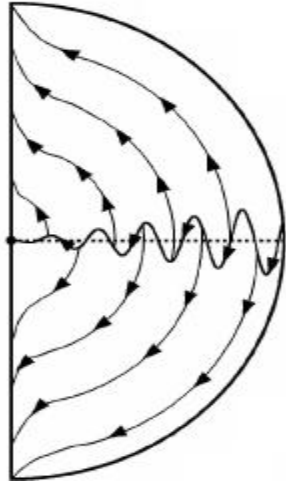
$$j(r, E, t) = p^2 f(r, p, t)$$



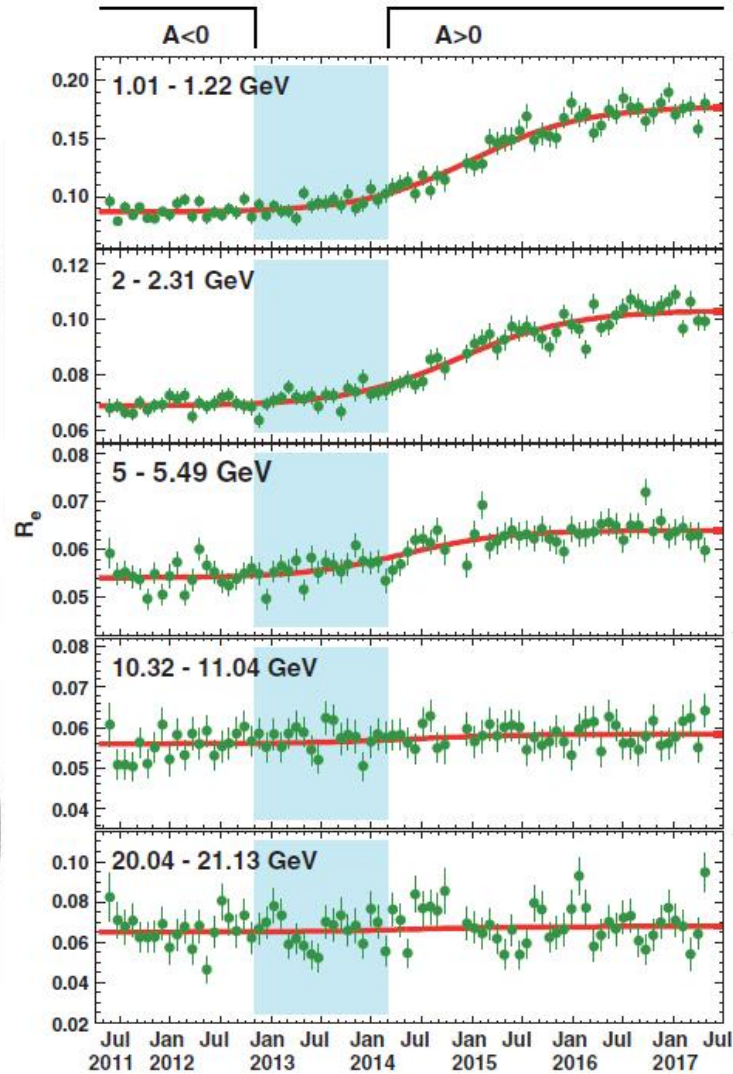
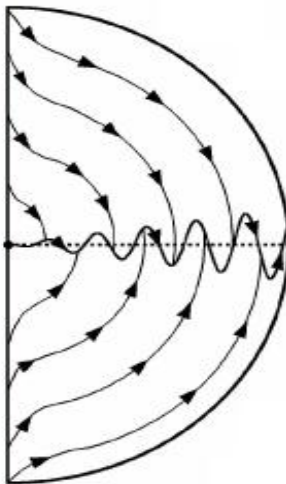
1. Convection: The outwards moving solar wind advects the magnetic field and cosmic rays.
2. Diffusion: Scattering by **the irregularity** of the magnetic field cause the cosmic ray diffuse.
3. drift : Large scale spatial variation of the average magnetic field cause coherent guiding-center drifts (gradient, curvature and current sheet).
4. adiabatic energy change : the expansion and compression of solar wind  $\nabla \cdot V$  causes the cosmic ray particles lose or gain energy.

# The Drift Effect: Charge-Sign Dependent Modulation

Drift direction of electrons in  $A > 0$  cycle

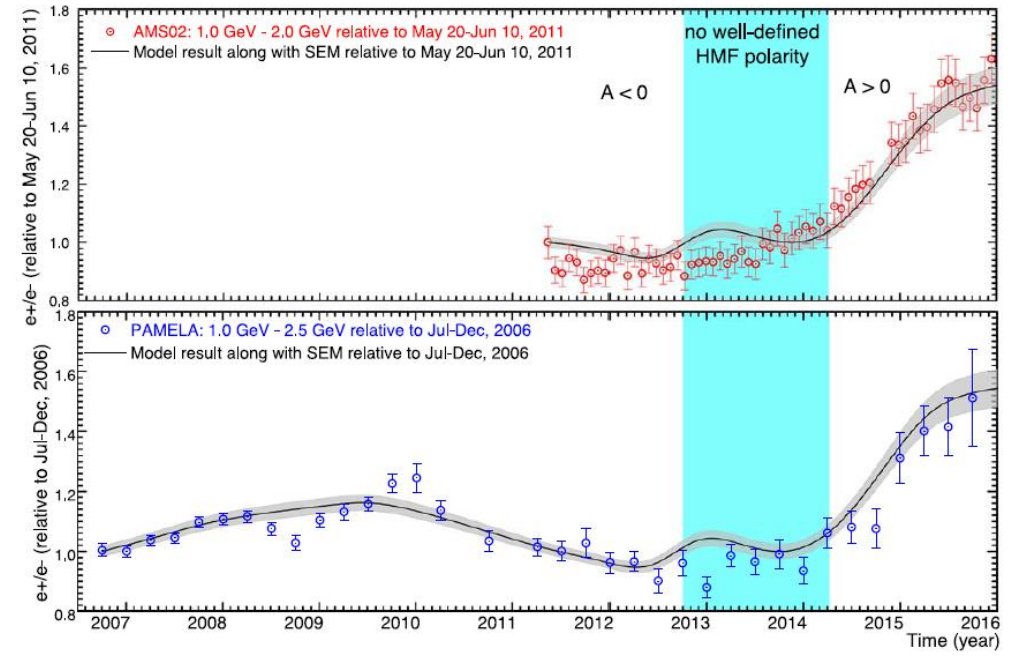


Drift direction of electrons in  $A < 0$  cycle

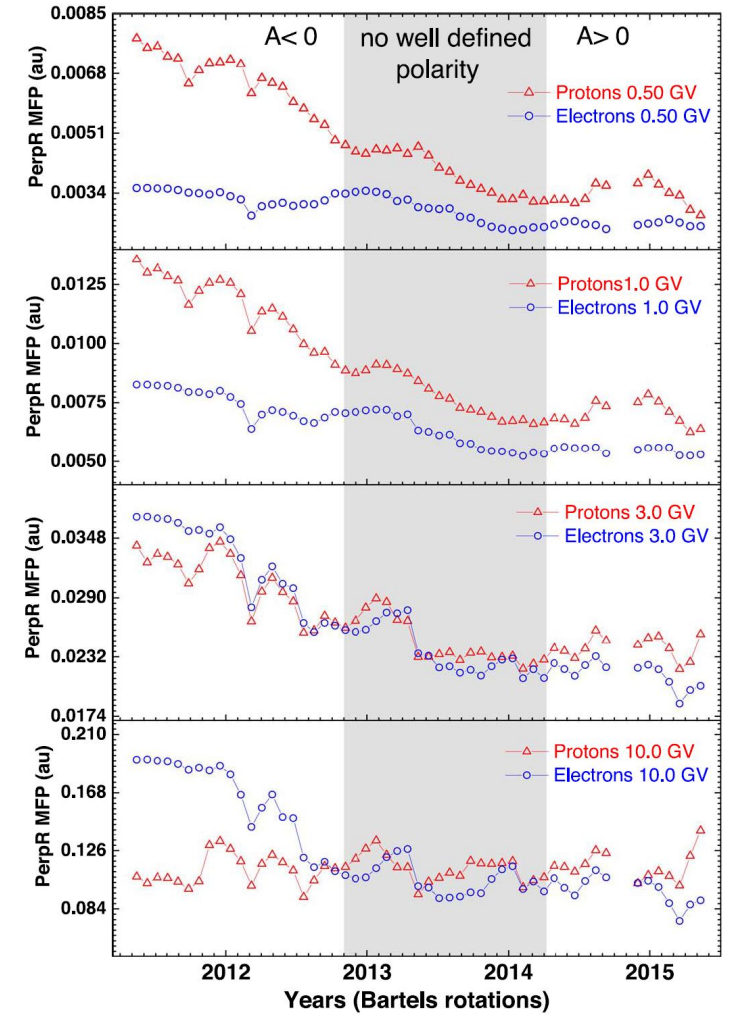
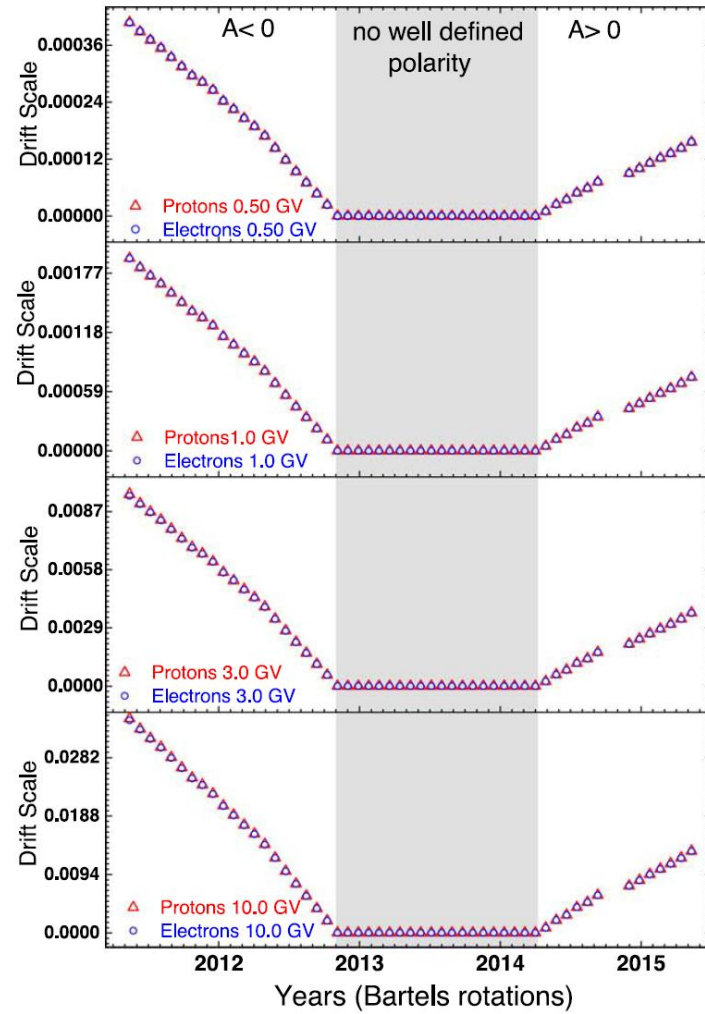
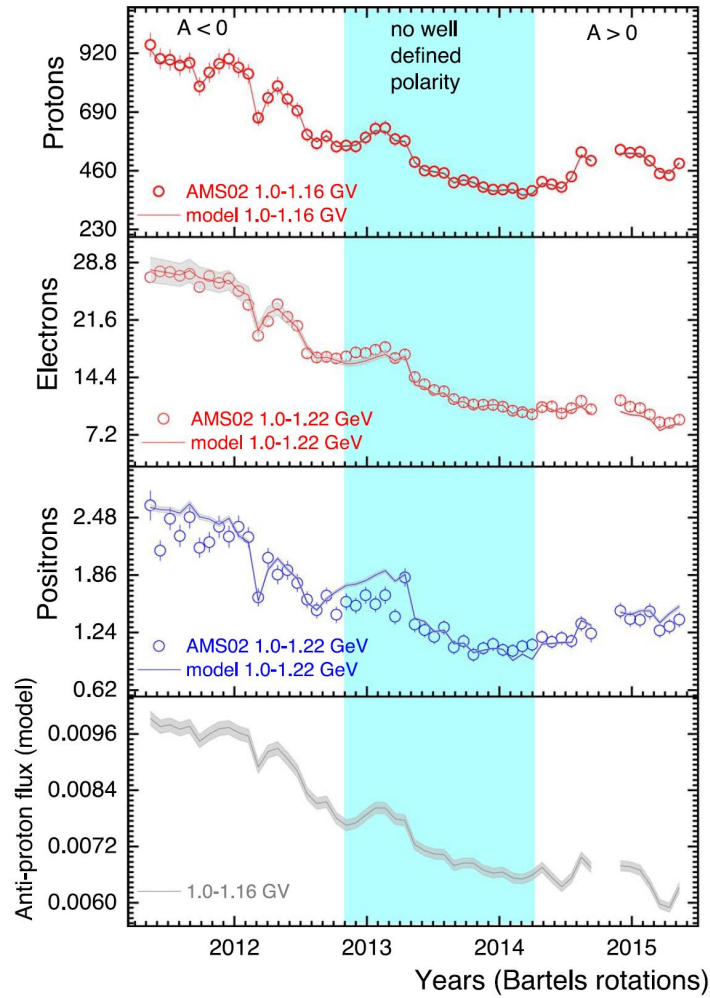


Aguilar M. et al. PRL 2018

The positron to electron ratio rises after the Solar Magnetic Field polarity reverse from  $A < 0$  to  $A > 0$ .

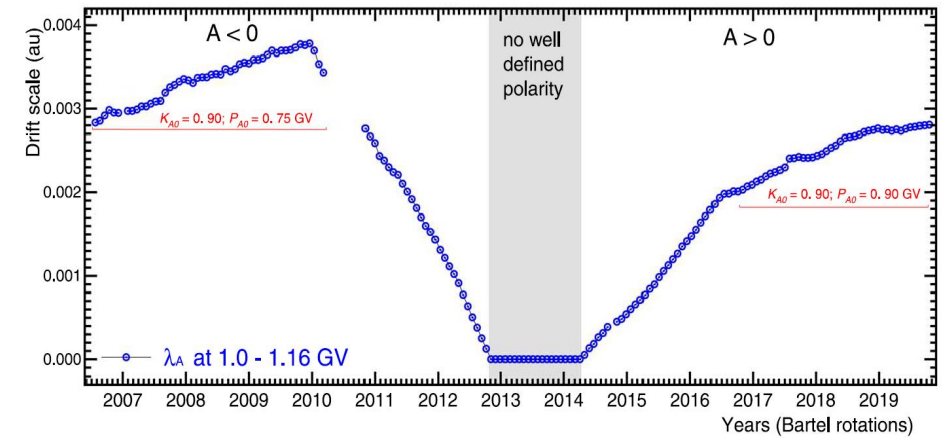
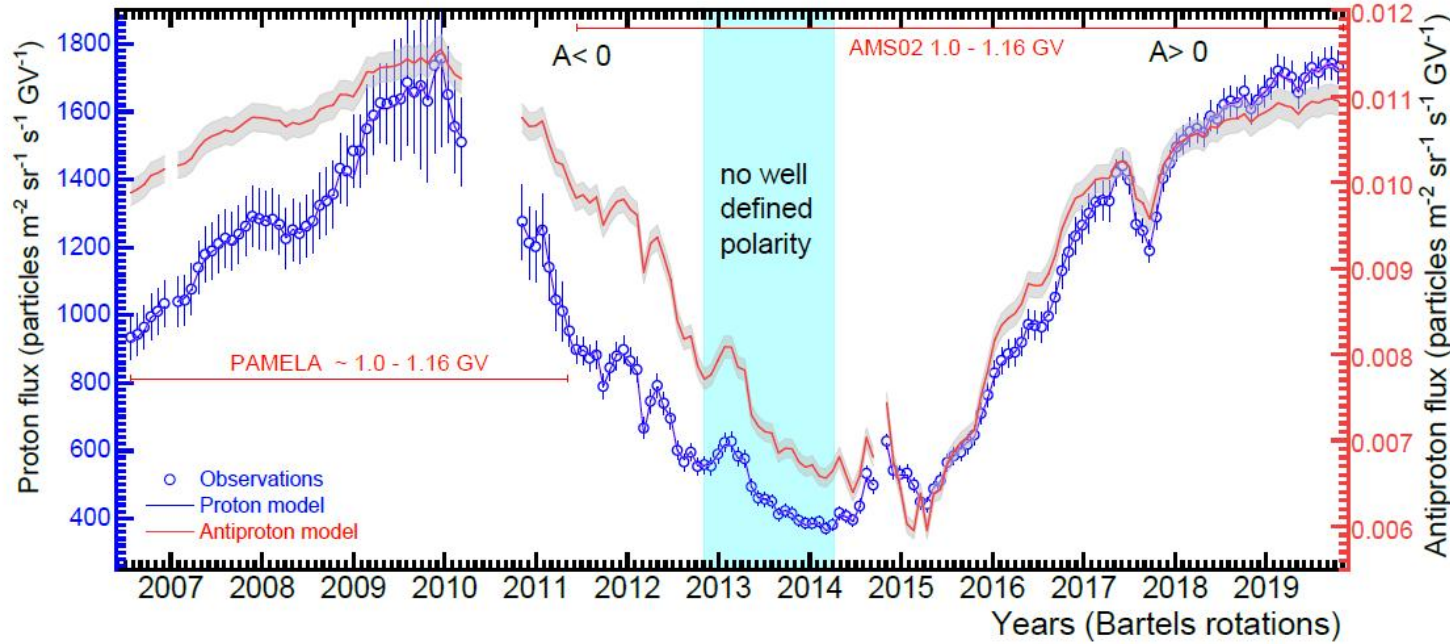


# Solar Modulation During Solar Magnetic Polarity Reversal

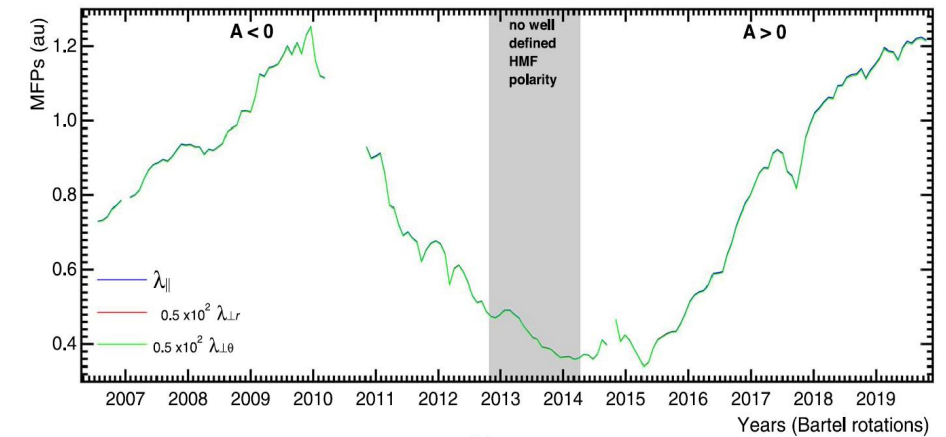


Aslam et al., ApJ, 2023,  
947,72

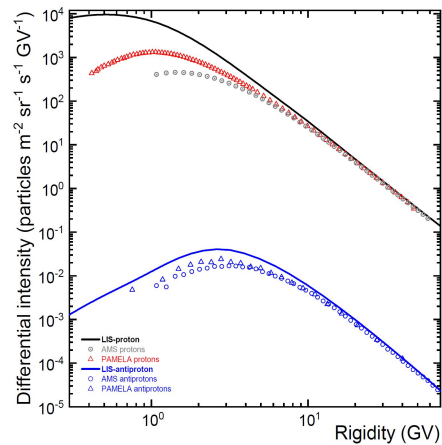
# Solar Modulation During Solar Magnetic Polarity Reversal



(a)

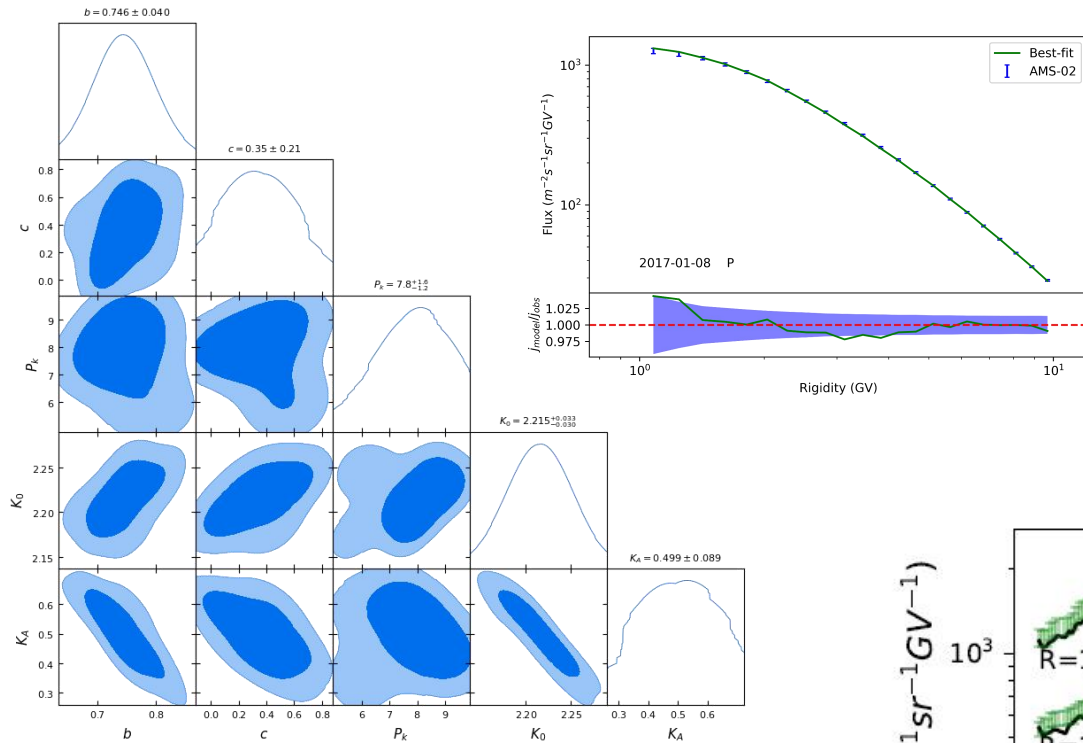


(b)



Aslam et al., ApJ, 2023,  
953,101

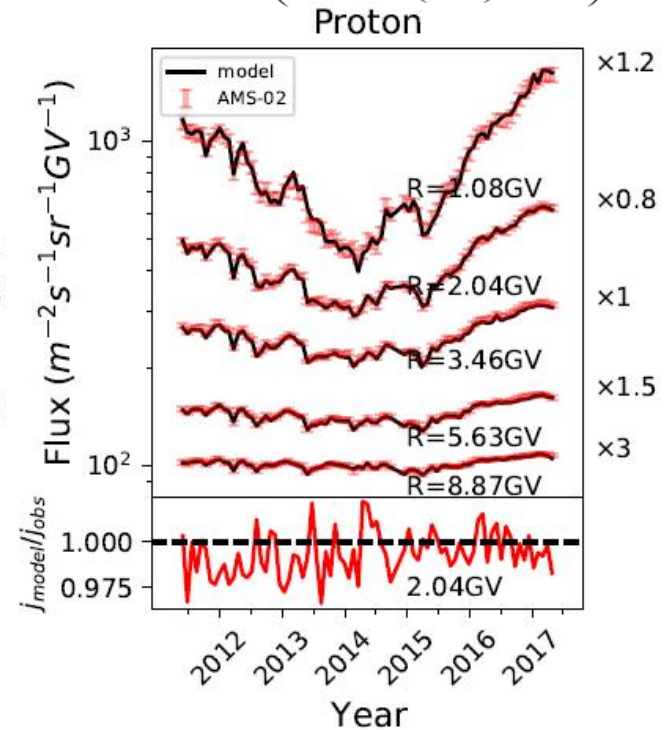
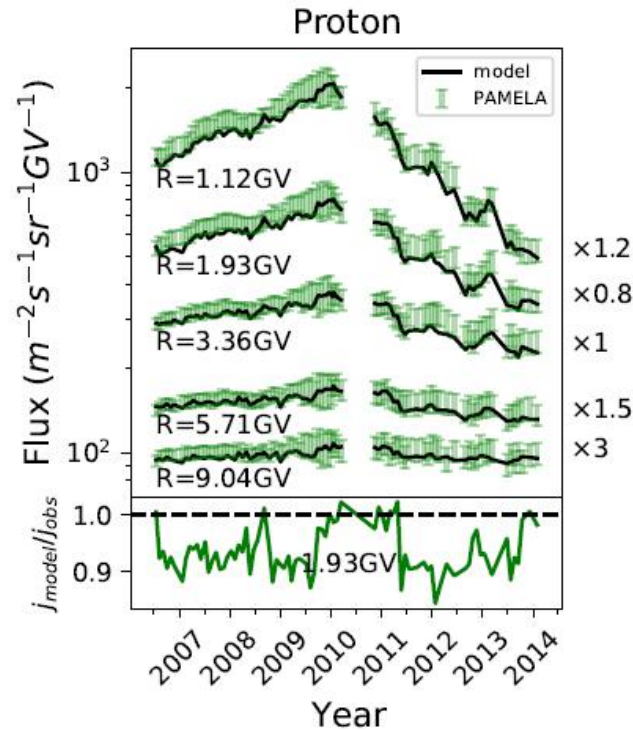
# GCR 11 Year Long-term Solar Modulation: Reproduce AMS Proton Observation



$$v_d = \nabla \times \left( K_A \frac{qP\beta}{3B} \frac{(P/P_0)^2}{1+(P/P_0)^2} \frac{\bar{B}}{B} \right)$$

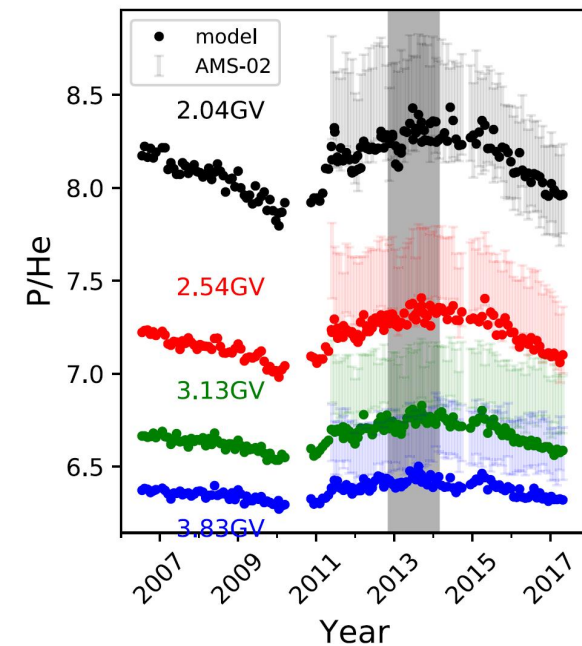
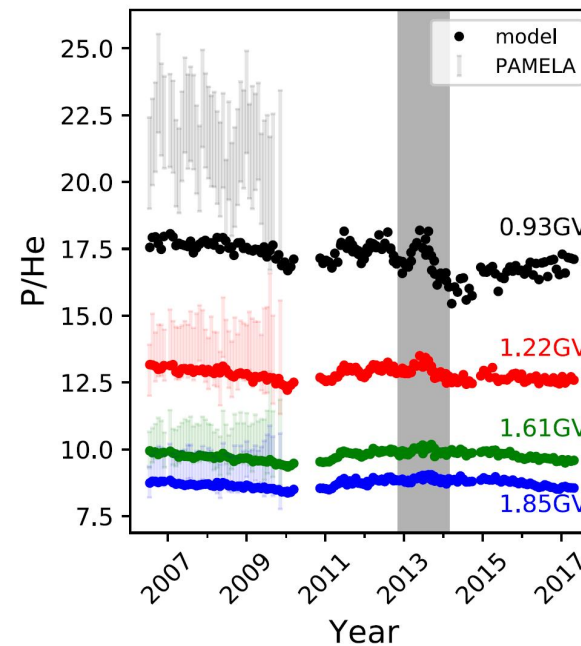
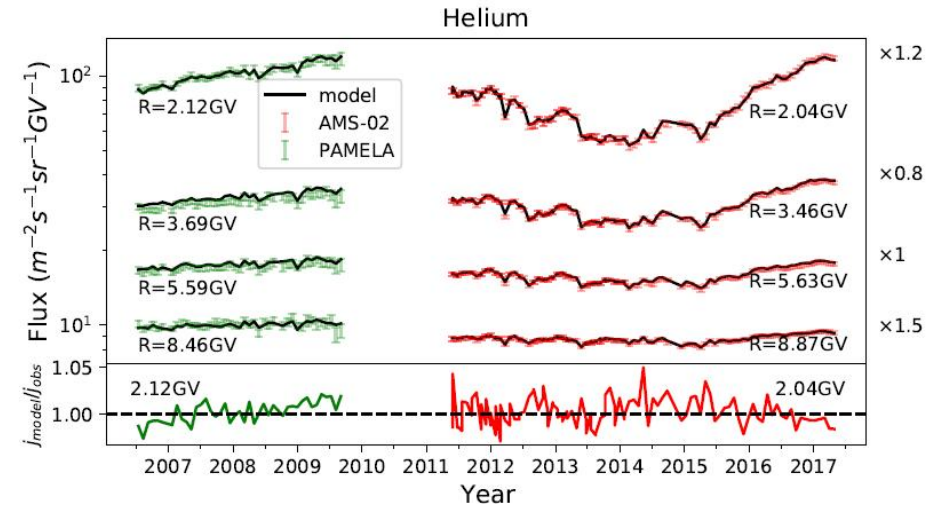
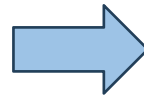
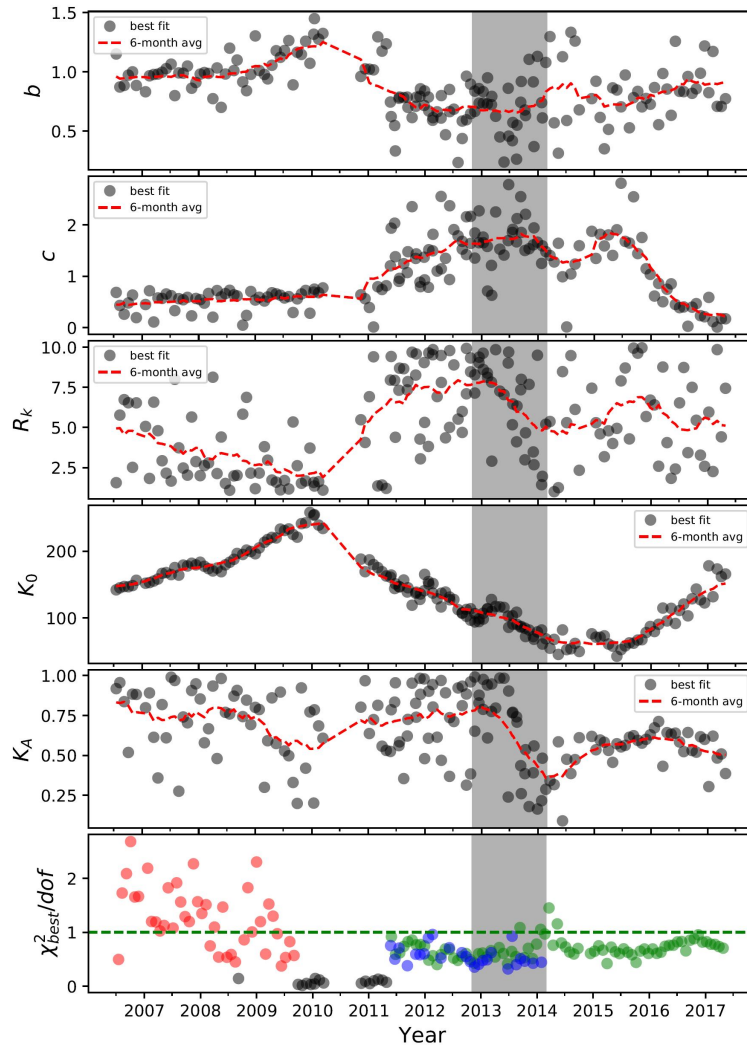
$$K_{\parallel} = K_0 \left( \frac{B_{eq}}{B} \right) \left( \frac{P}{P_0} \right)^b \left( \frac{\left( \frac{P}{P_0} \right)^d + \left( \frac{P_k}{P_0} \right)^d}{1 + \left( \frac{P_k}{P_0} \right)^d} \right)^{\frac{c-b}{d}}$$

Song, Luo+, 2021, ApJS

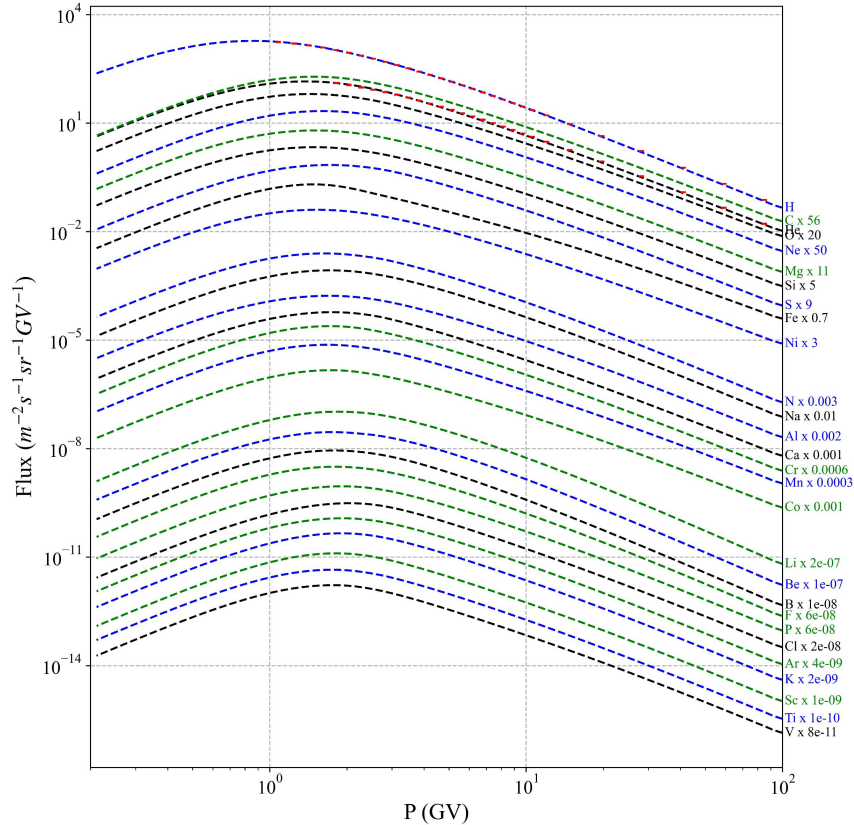


# Reproduce AMS Helium Observation

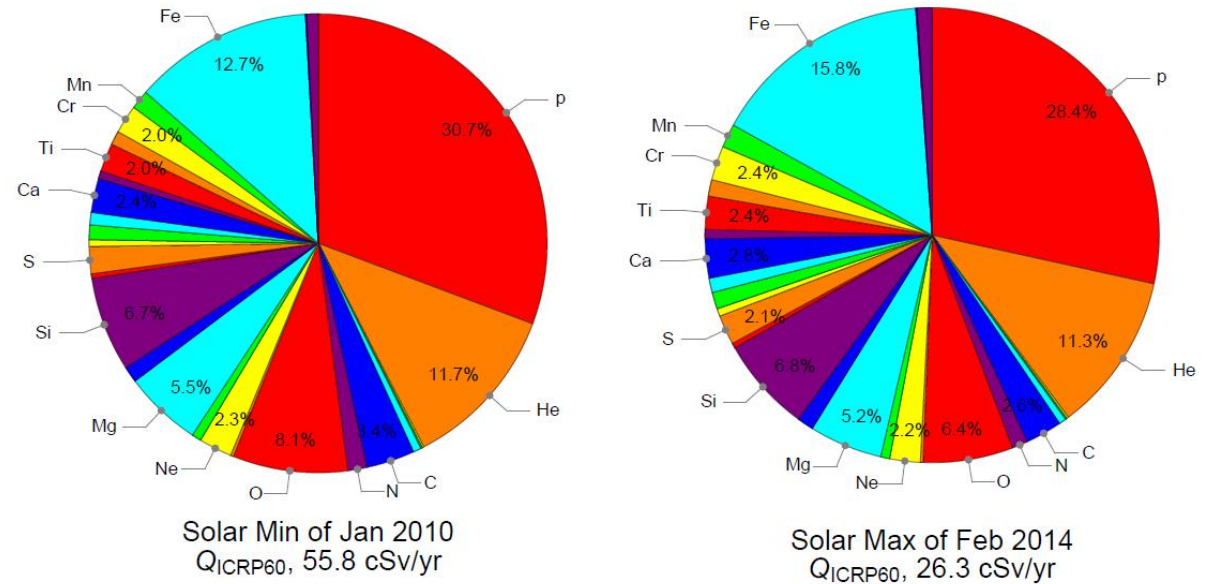
The same set of modulation parameters are utilized to reproduce Helium flux variation.



# Convert GCR Spectra to Radiation Dose



## Contribution from Elements: $w_T$ Weighted



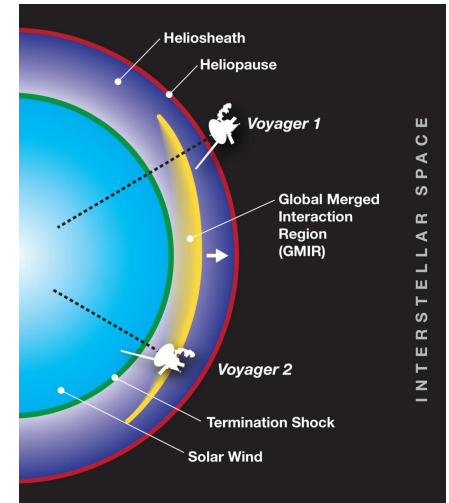
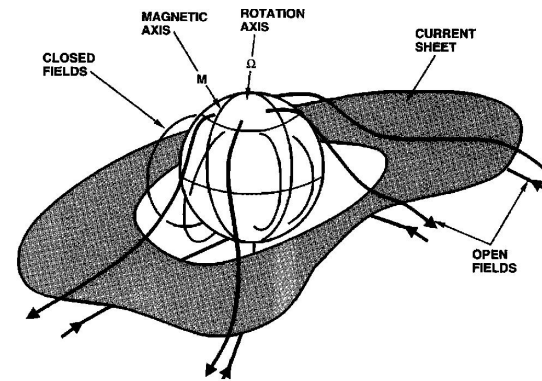
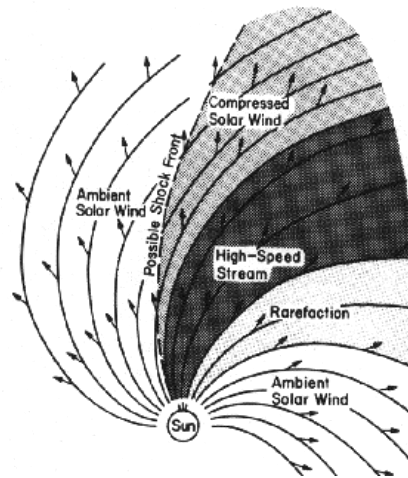
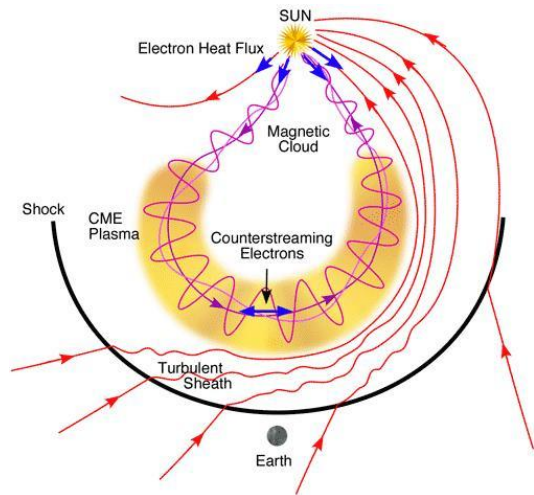
Chen, X., Xu, S., Song, X., Huo, R., & Luo, X. (2023). *Space Weather*, 21

The same set of modulation parameters are utilized to reproduce GCR spectra (From Z=1 to Z=26).

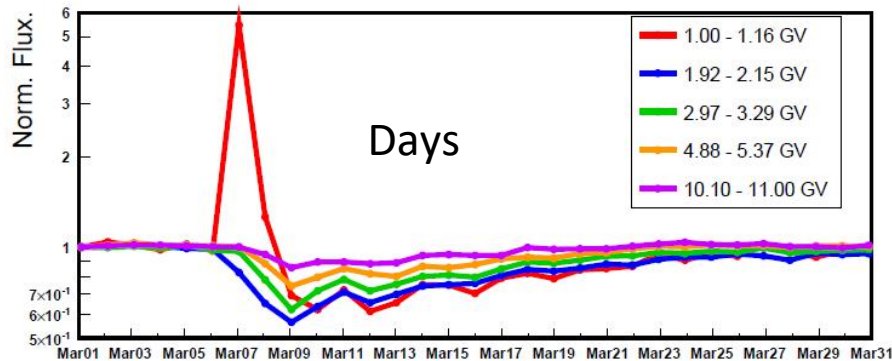
$$H_T = \sum_R \int dE 4\pi J_R(E) (D_{T,R}/\Phi)(E) Q$$

# GCR Short-term Solar Modulation

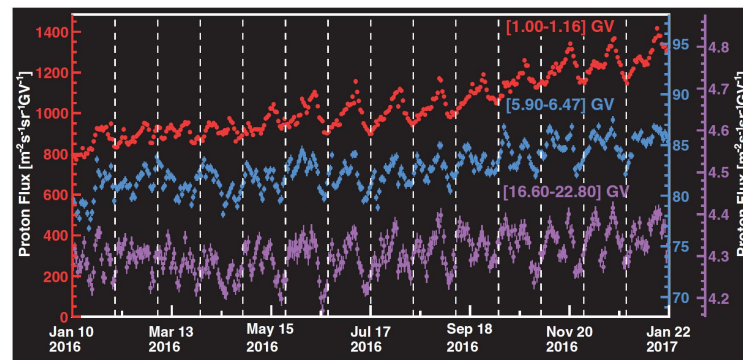
## Various Solar Wind Plasma Structures



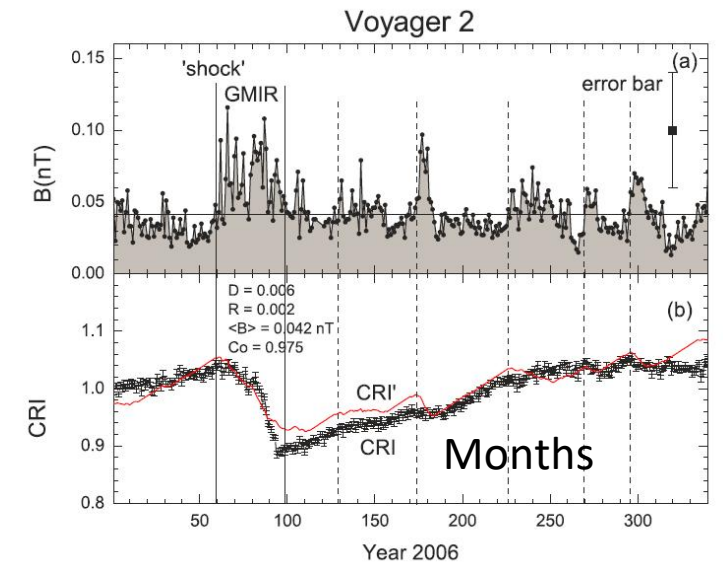
Weeks



Consolandi et al., 2015

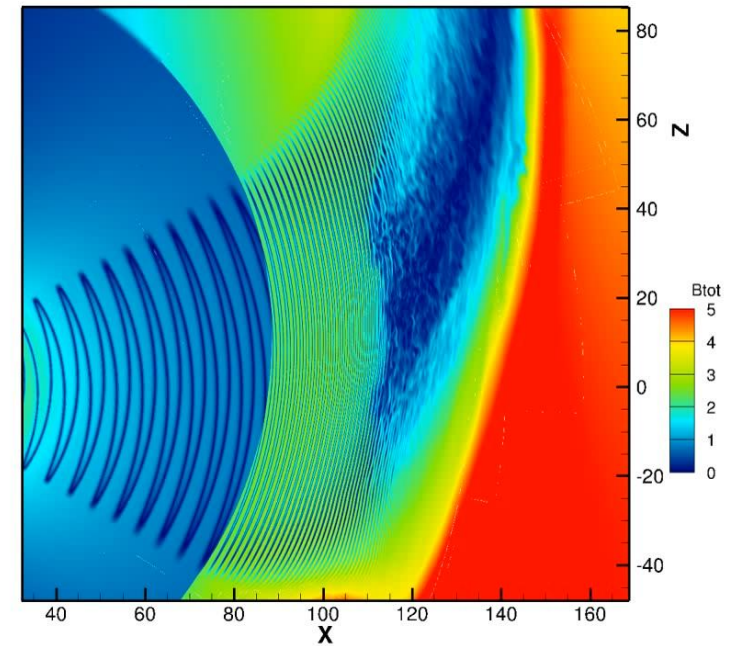
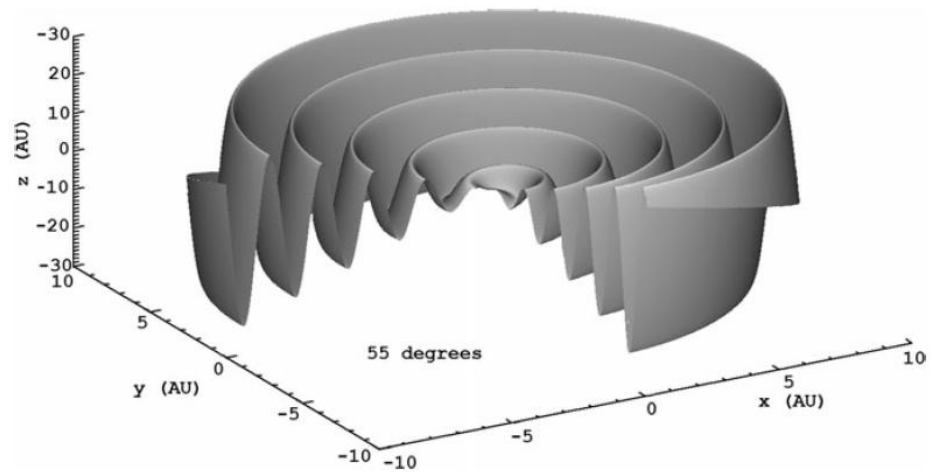
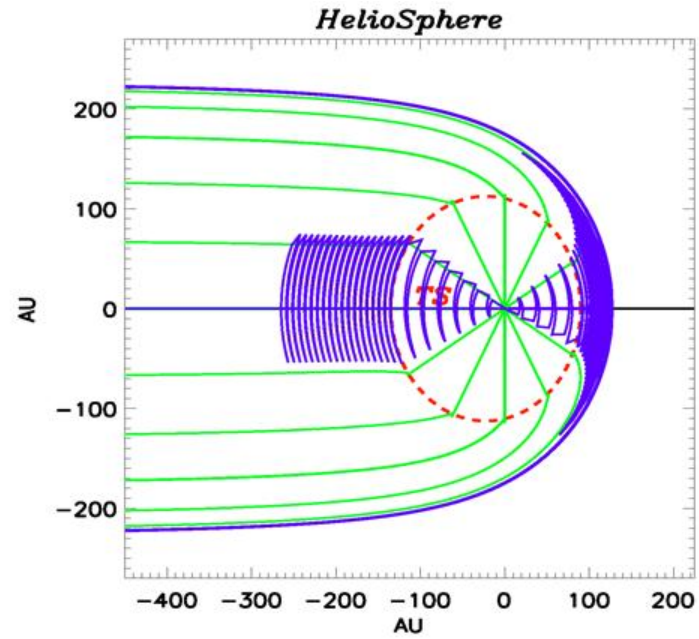
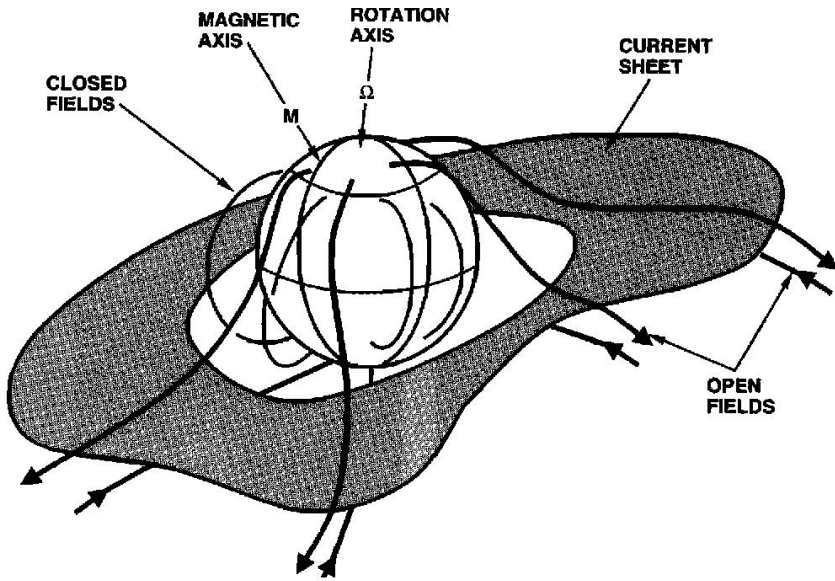


Aguilar M. et al. 2021

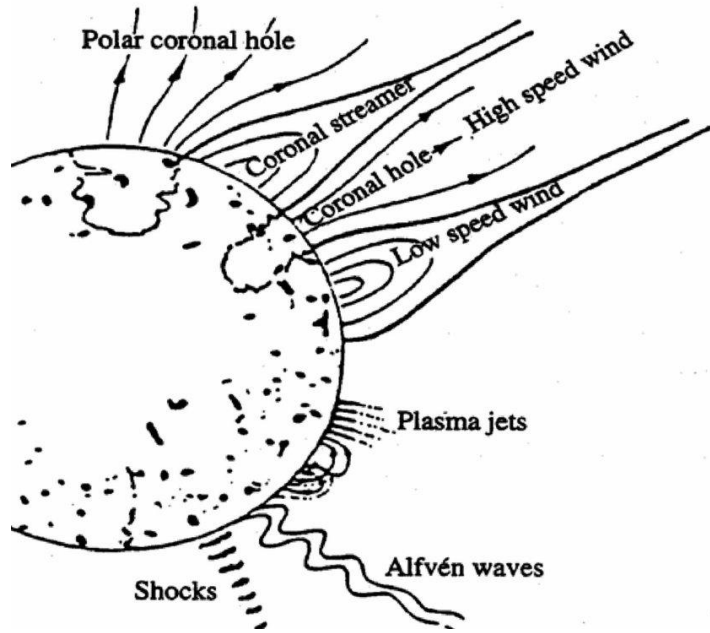


Burlaga et al. 2013

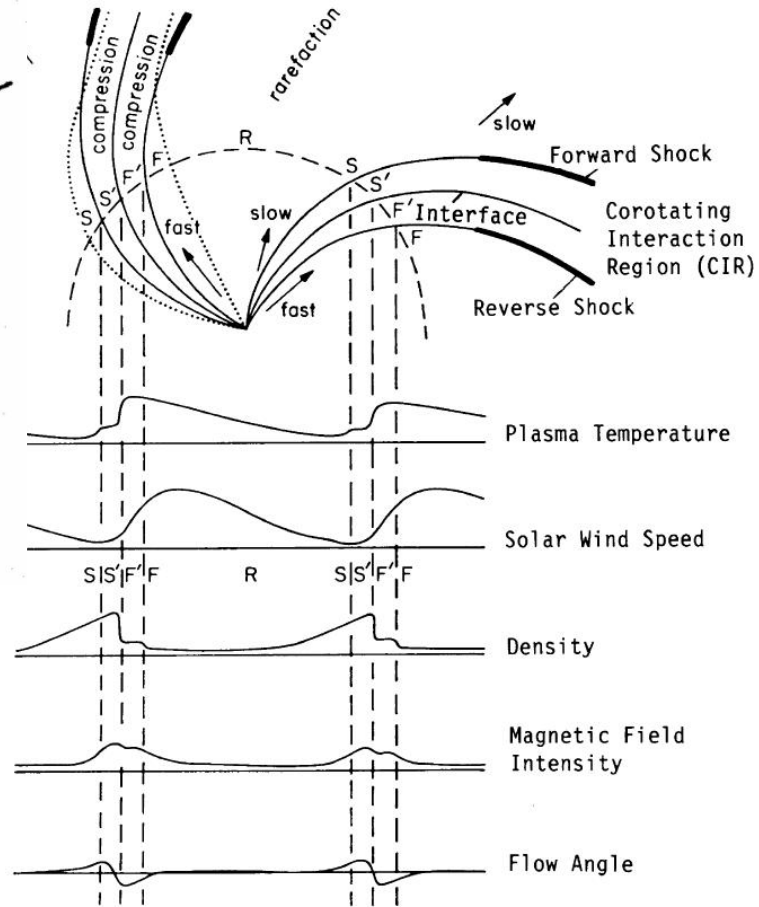
# Heliosphere Current Sheet



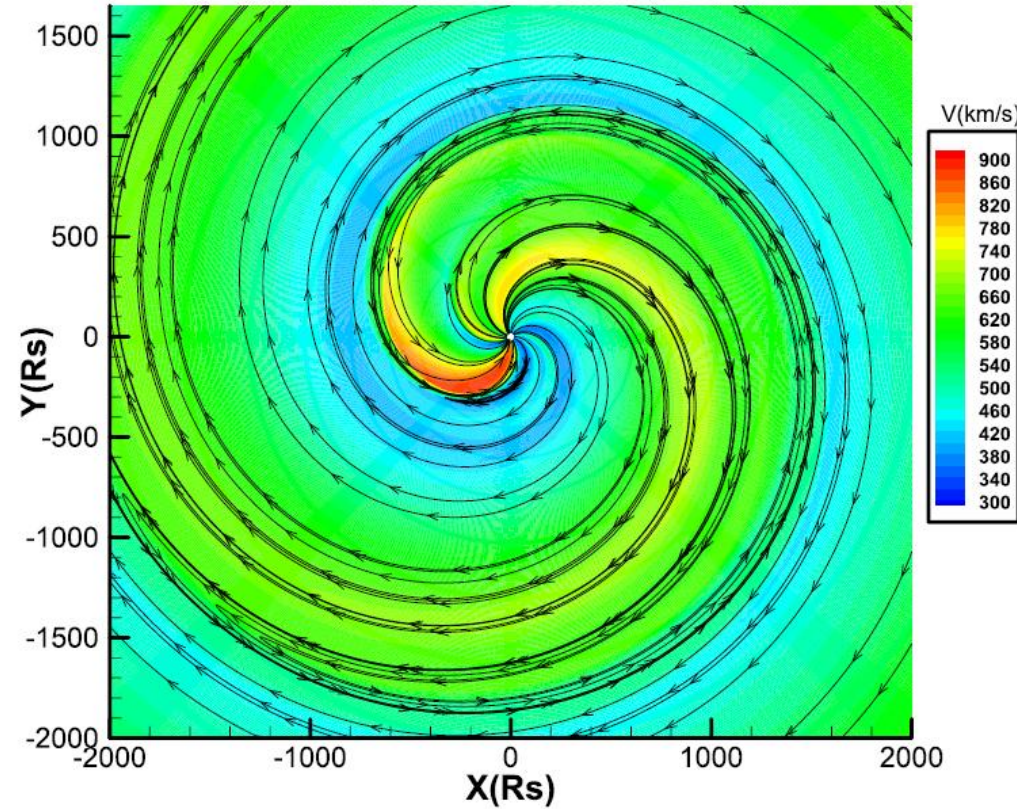
# Corotating Interaction Region



Dryer et al. (1987)



Belcher and Davis (1971)

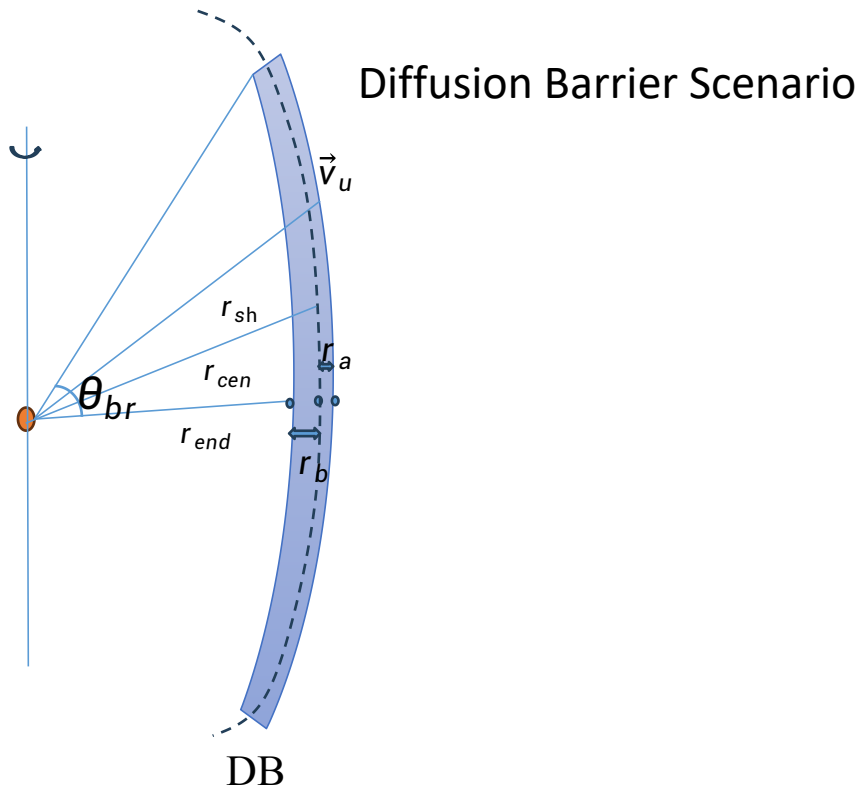


Luo et al. (2020)

$$\psi = \arctan(r\Omega/V)$$

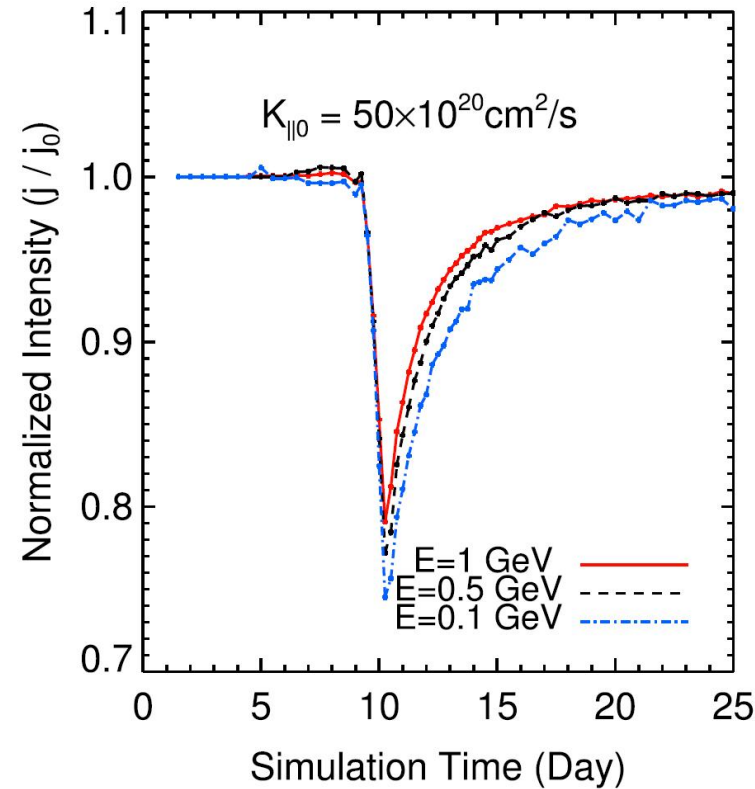
According to the Parker theory, The fast solar wind stream gets less twisted.

# GCR Short-term Solar Modulation: Forbush Decrease Events



$$\frac{\rho_2}{\rho_1} = 1 + \rho f(r) h(\theta) g(\phi)$$

$$K'_{\parallel, \perp} = \frac{K_{\parallel, \perp}}{1 + \rho f(r) h(\theta) g(\phi)}$$



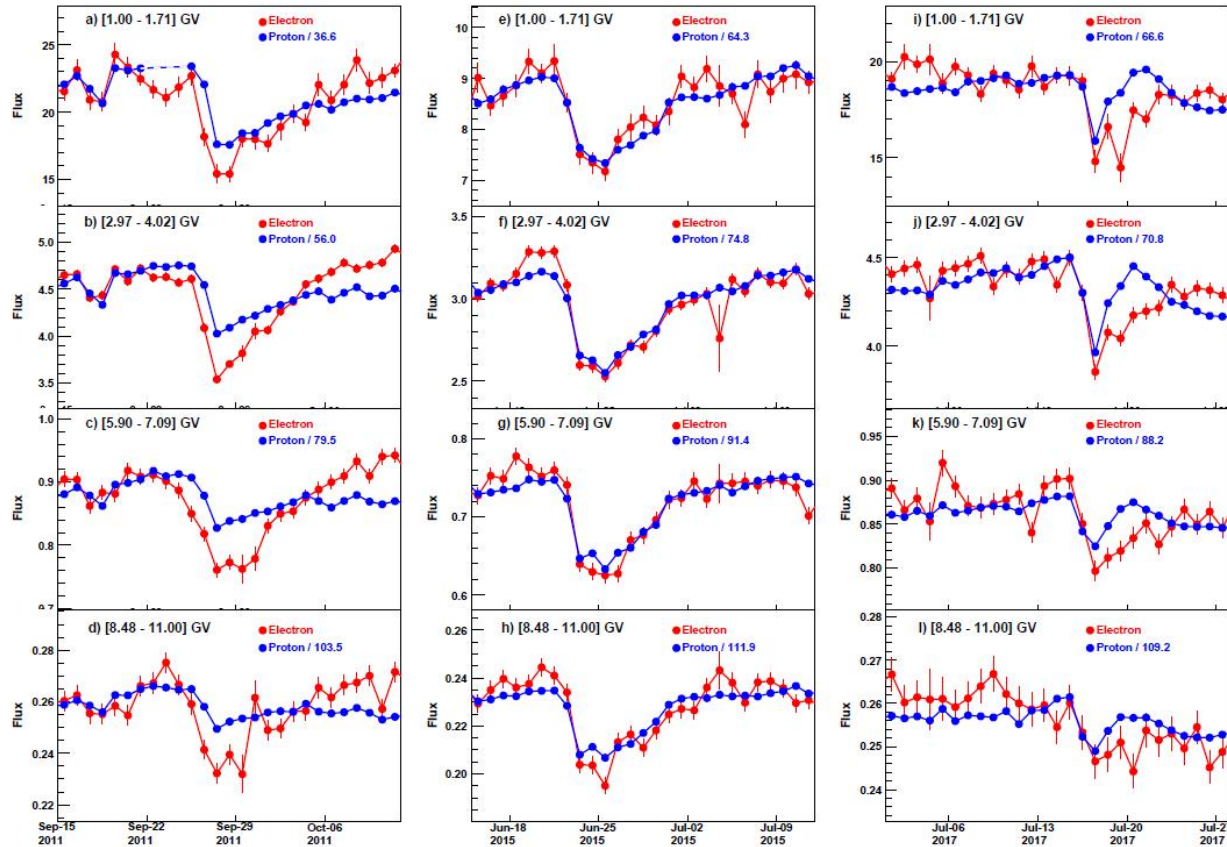
DAMPE 实验数据

Recovery time  
energy  
dependence

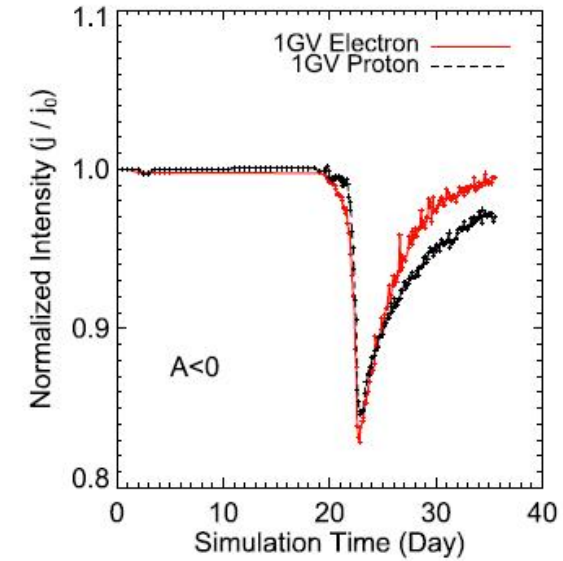
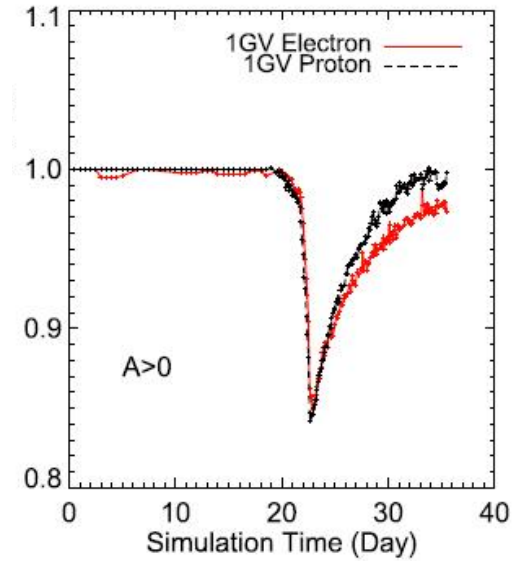
The energy dependence.

Luo+, et al., ApJ, 2017

# GCR Short-term Solar Modulation: Forbush Decrease Events

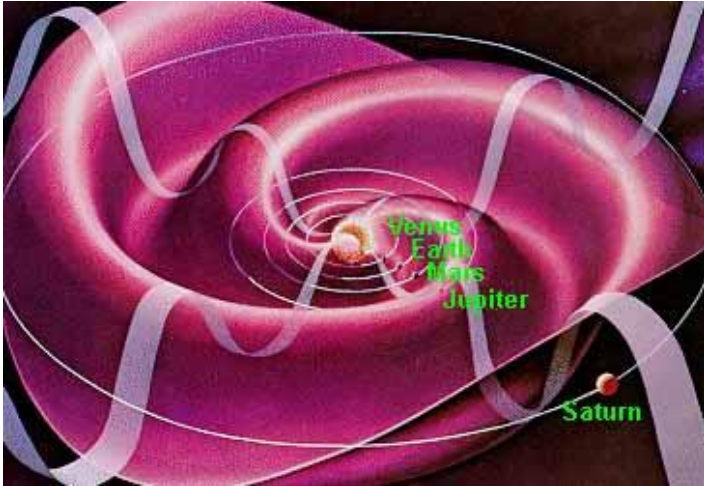


The charge-sign dependence.



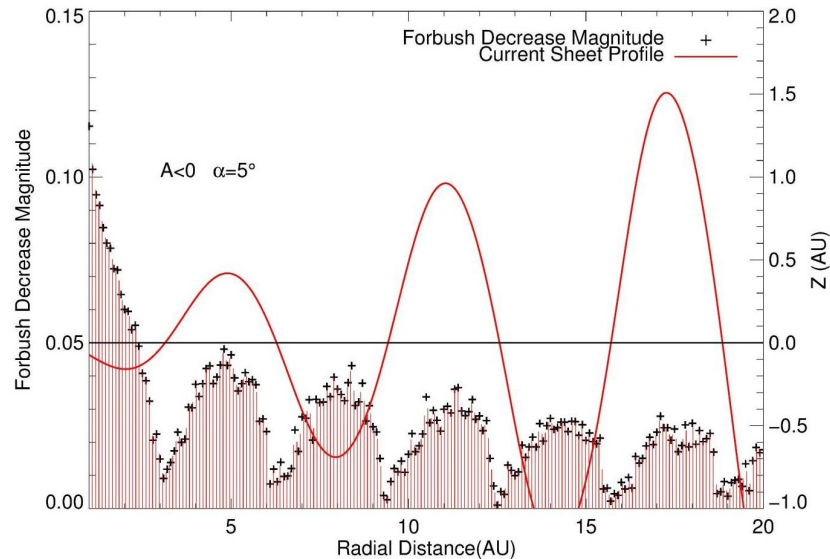
Luo+, et al., ApJ, 2018

# GCR Short-term Solar Modulation: Forbush Decrease Events

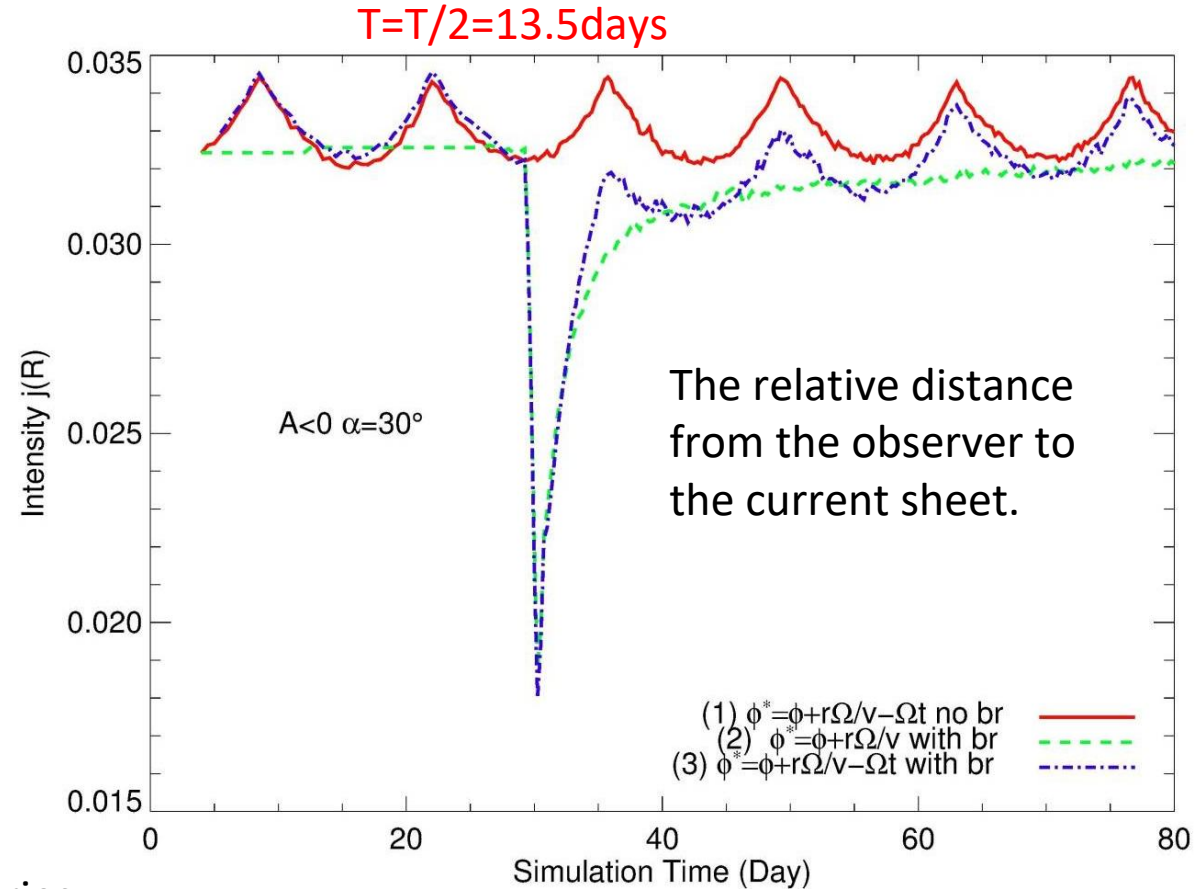


$$-\cot(\theta_{cs}) = \tan \alpha \sin(\phi^*)$$

$$\phi^* = \phi + \frac{r\Omega}{V_{sw}} - \Omega t$$



Fd magnitude varies with distance.



Luo, Xi, et al., ApJ, 2017

# GCR Short-term Solar Modulation: Corotating Interaction Region

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{V}) = 0$$

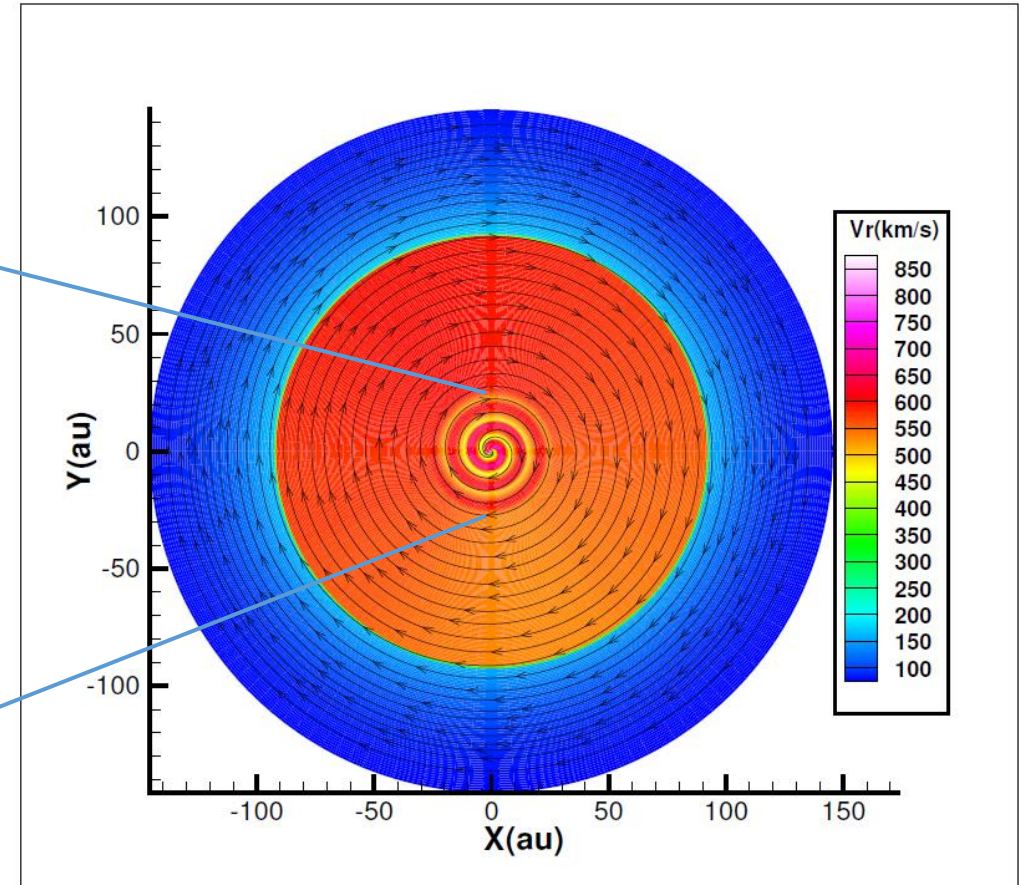
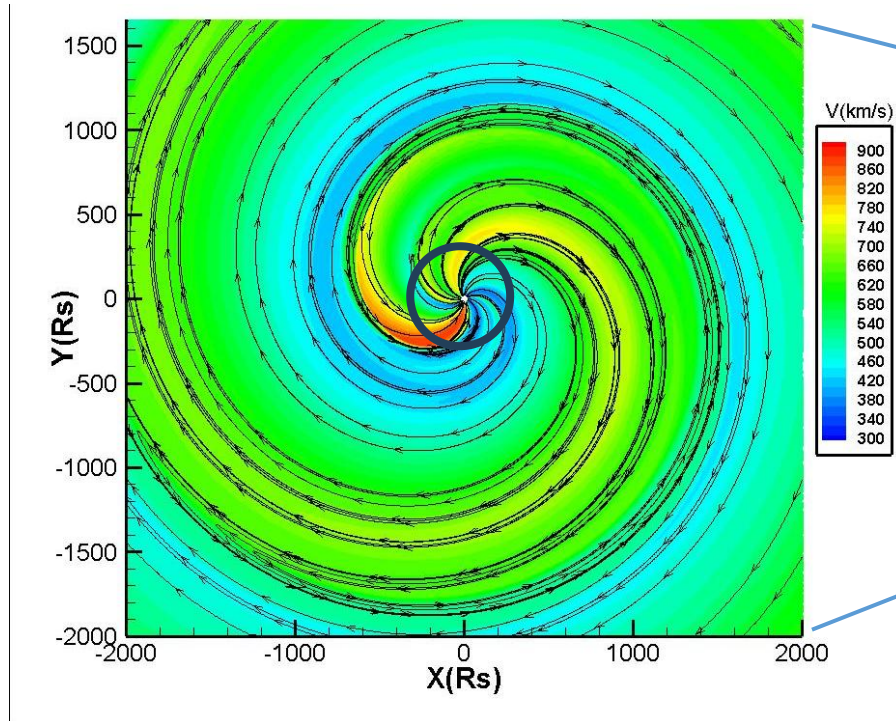
$$\frac{\partial \rho \mathbf{V}}{\partial t} + \nabla \cdot \left[ \left( P + \frac{B^2}{2\mu_0} \right) \mathbf{I} + \rho \mathbf{V} \mathbf{V} - \frac{B \mathbf{B}}{\mu_0} \right] = -\frac{\rho G M_s r}{r^2} + \mathbf{V} \cdot \mathbf{f}$$

$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{V} \mathbf{B} - \mathbf{B} \mathbf{V}) = 0$$

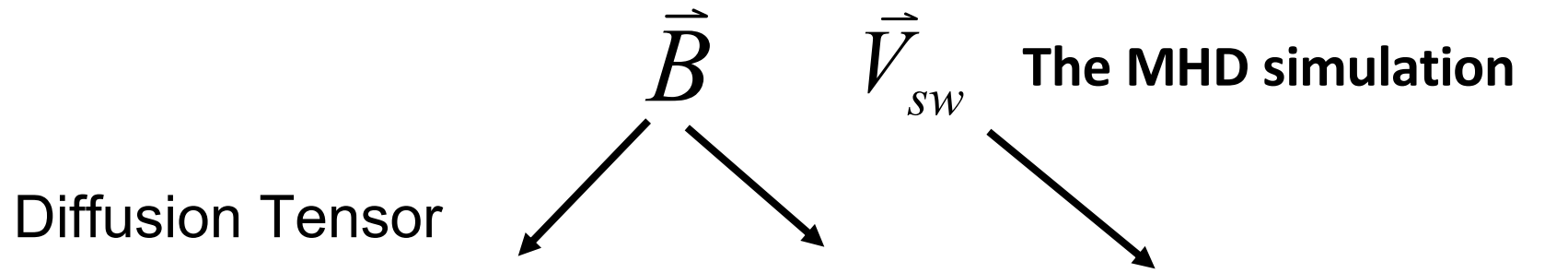
$$\frac{\partial P}{\partial t} + \nabla \cdot (\rho \mathbf{V}) = -(\gamma - 1) P \nabla \cdot \mathbf{V}$$

$((V_r, V_\theta, V_\phi), (B_r, B_\theta, B_\phi), N, P)$

Expressed in the solar co-rotating frame.



# GCR Short-term Solar Modulation: Corotating Interaction Region



$$\vec{\kappa} = \kappa_{\perp} \vec{I} + (\kappa_{\parallel} - \kappa_{\perp}) \hat{b}\hat{b}$$

$$\kappa_{\parallel} = K_0 \beta \left( \frac{B_{eq}}{B} \right) \left( \frac{R}{R_0} \right)^a \left( \frac{\left( \frac{R}{R_0} \right)^c + \left( \frac{R_k}{R_0} \right)^c}{1 + \left( \frac{R_k}{R_0} \right)^c} \right)^{\frac{b-a}{c}}$$

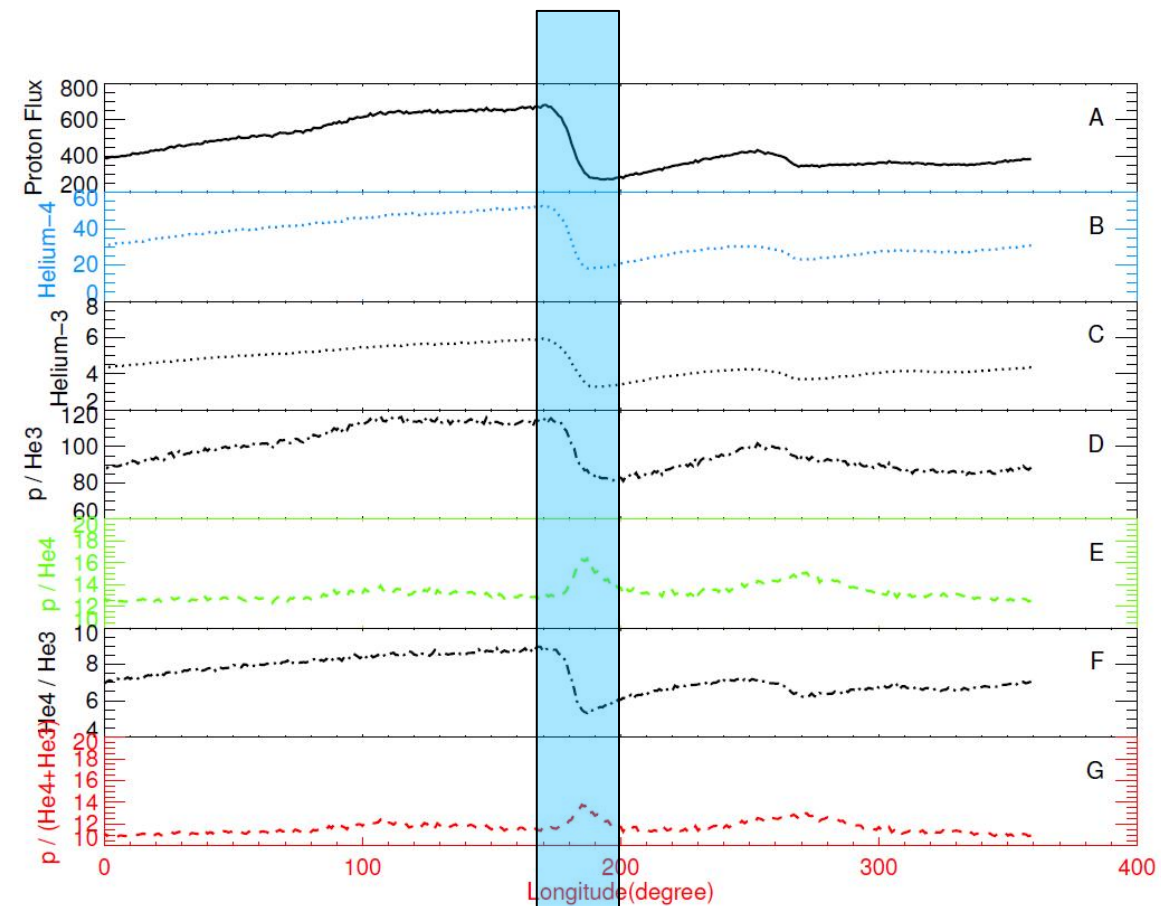
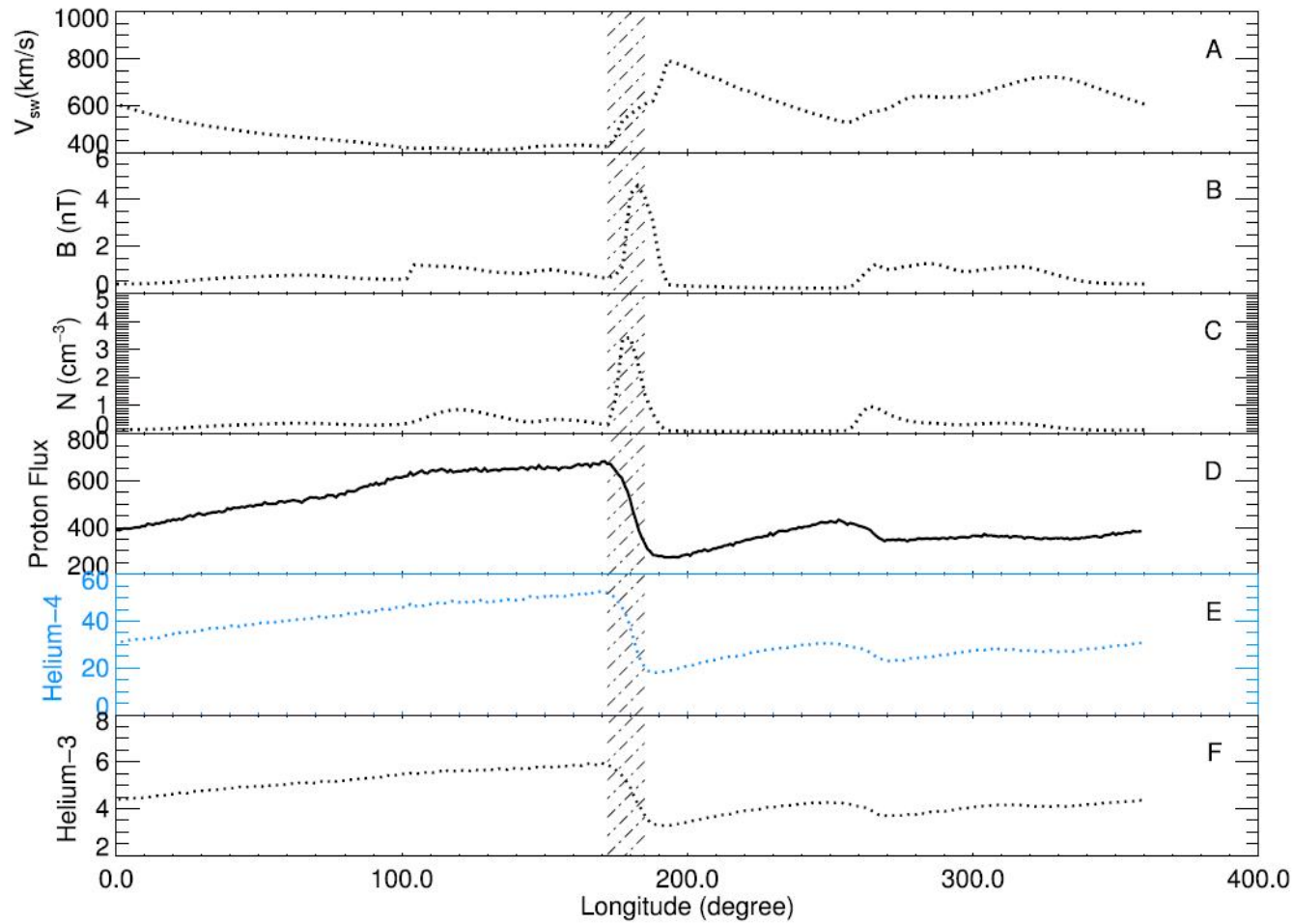
$K_{\perp, r, \theta} = 0.02 K_{\parallel}$

$$\langle \vec{v}_D \rangle = (K_d)_0 \frac{pv}{3q} \nabla \times \left( \frac{\vec{B}}{B^2} \right) \quad \vec{V}_{sw}$$

$$d\vec{x} = \sqrt{2} \vec{\kappa} \cdot d\vec{w}(s) + (\nabla \cdot \vec{\kappa} - \vec{V}_{sw} - \vec{V}_d) ds$$

$$dp = \frac{1}{3} \nabla \cdot \vec{V}_{sw} p ds$$

# GCR Short-term Solar Modulation: Corotating Interaction Region

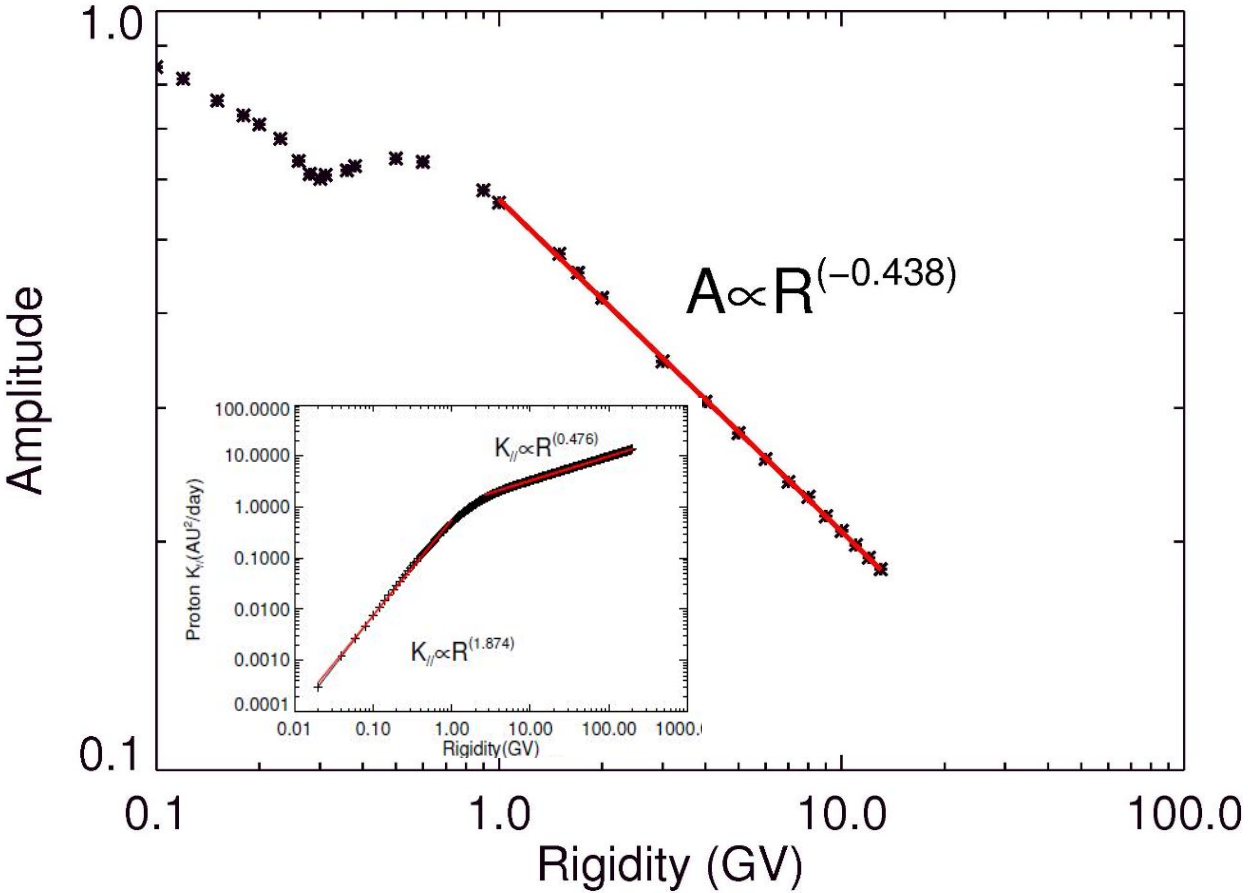
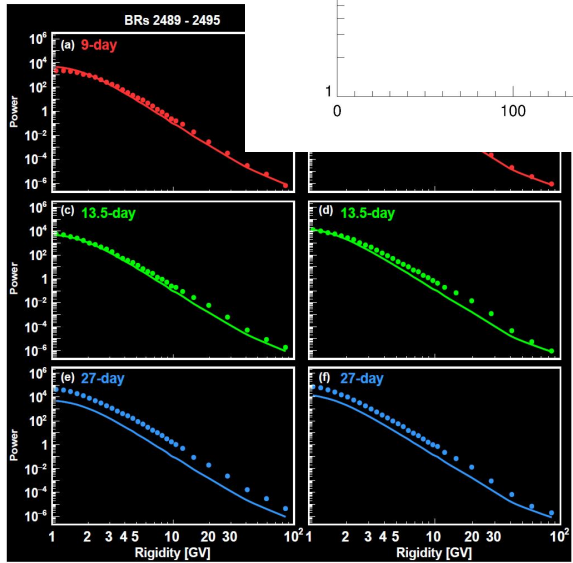
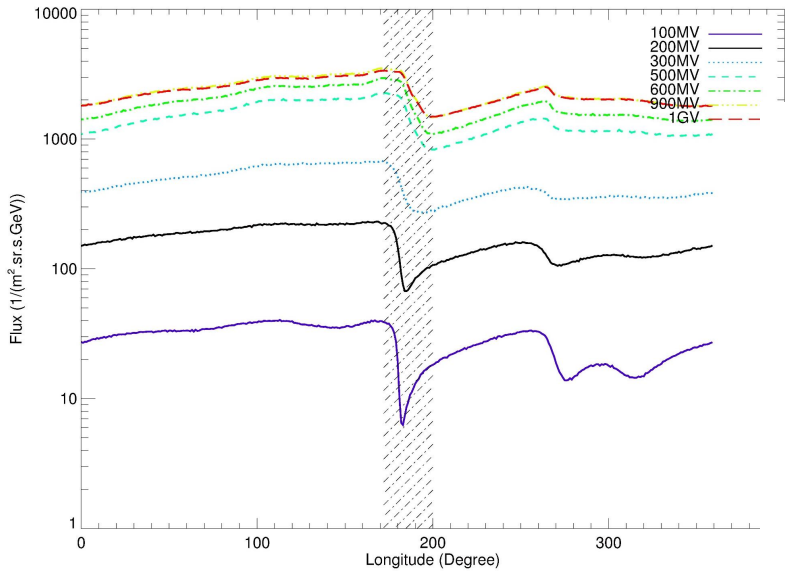


Luo, Xi, et al., ApJ, 2024

# GCR Short-term Solar Modulation: Corotating Interaction Region

## Region

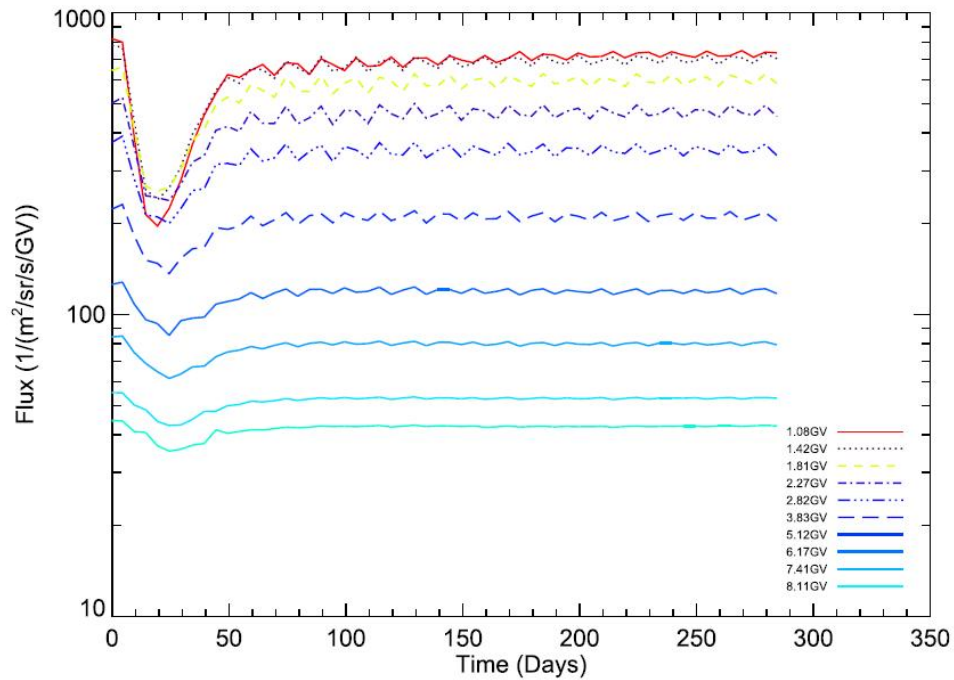
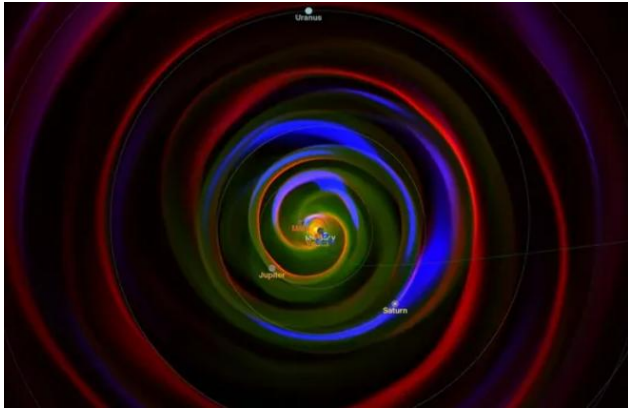
The effect of CIR on GCR proton exhibits rigidity dependence.



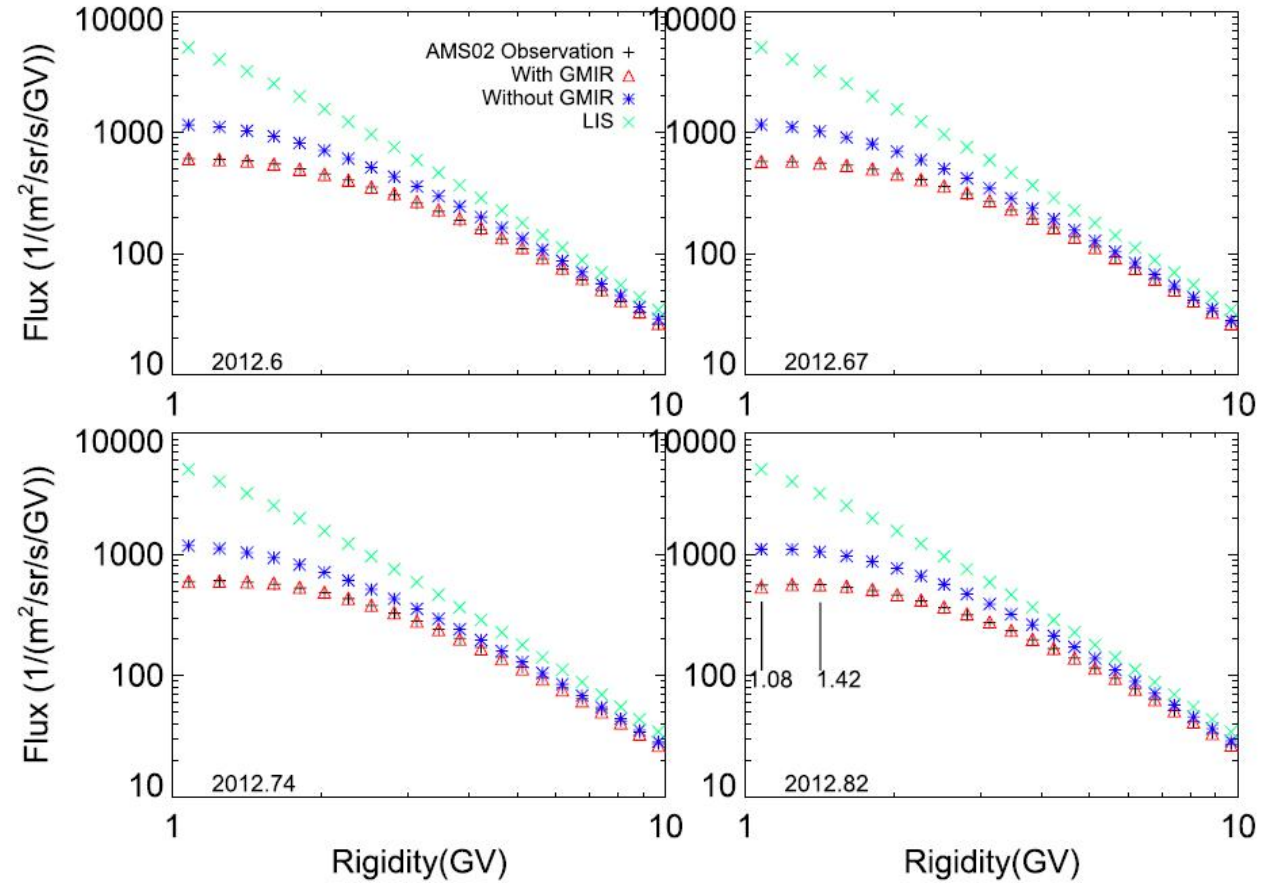
AMS observation Physical Review Letters 127, 271102 (2021)

Luo, Xi, et al., ApJ, 2024

# GCR Short-term Solar Modulation: Global Merged Interaction Region



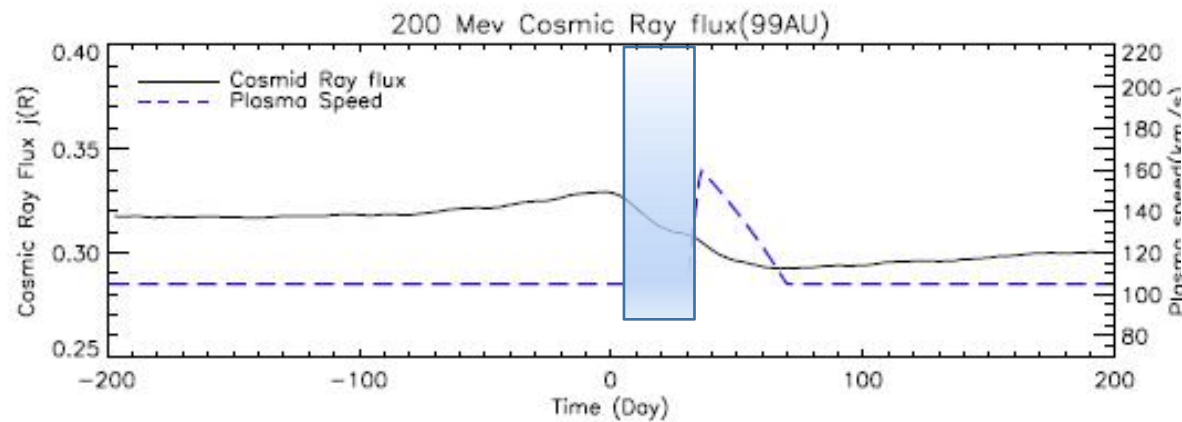
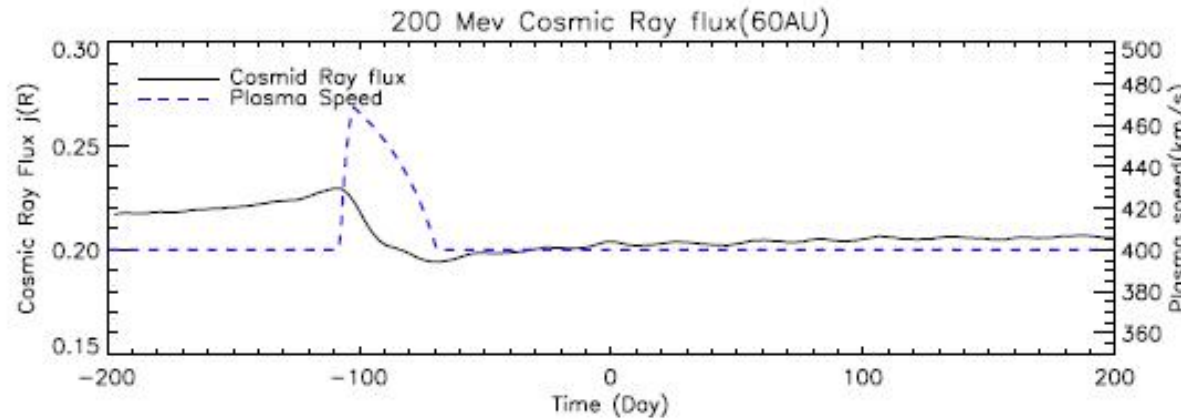
## Region



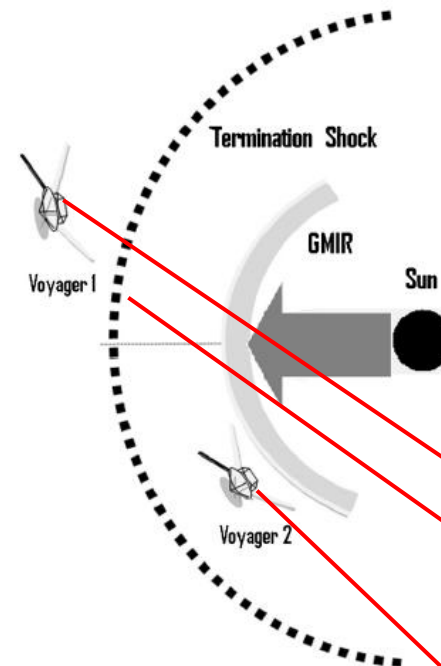
GMIR event at 1 au. (2012 July)

Luo+ ApJ 2019

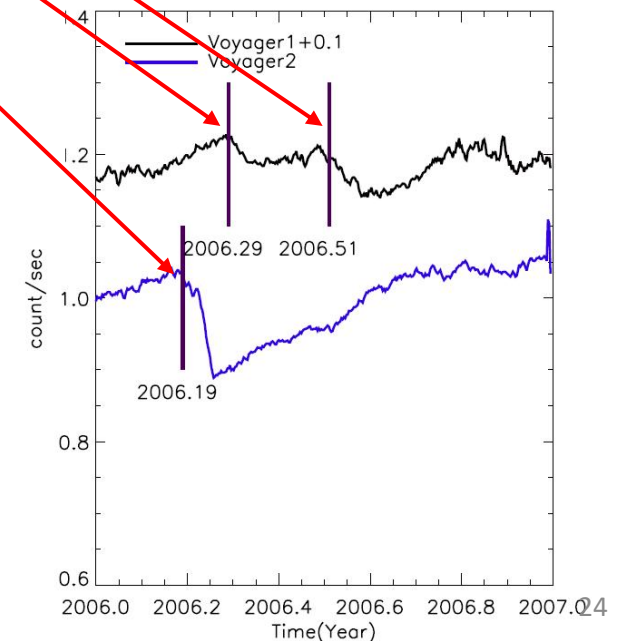
# GCR Short-term Solar Modulation: Global Merged Interaction Region



The GCR “remote sense” the interaction between the GMIR and Termination Shock.

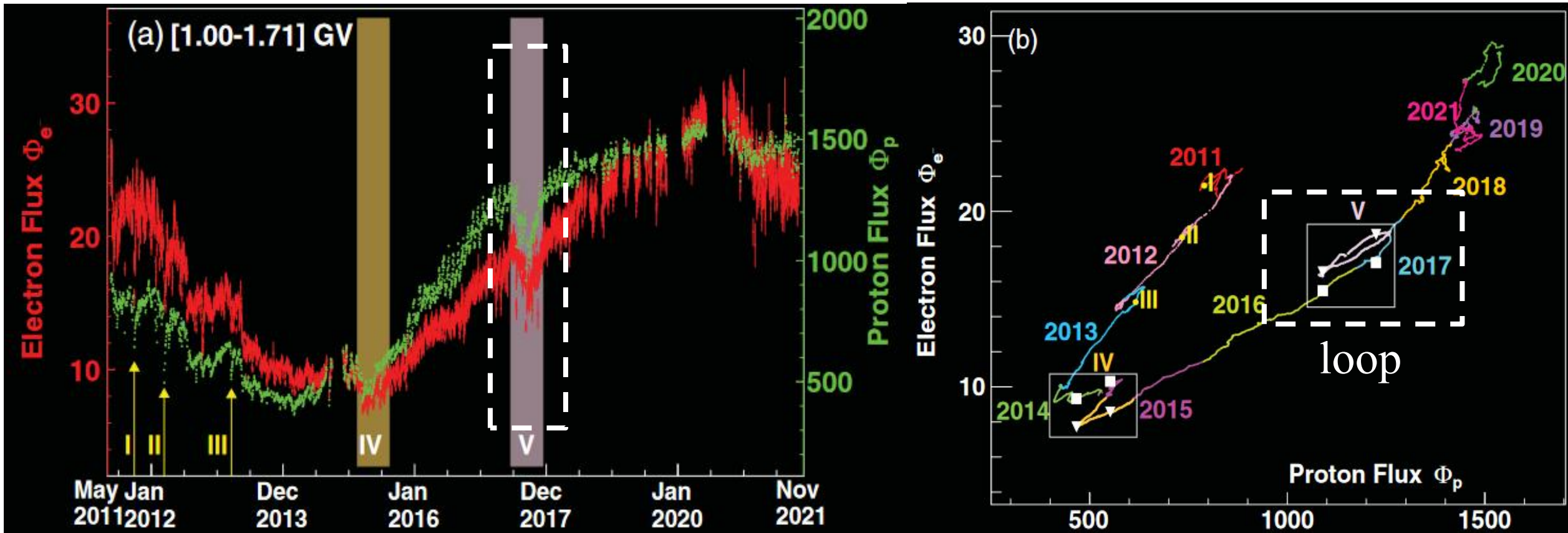


This effect has been observed by Voyager 1 in Mar. 2006.

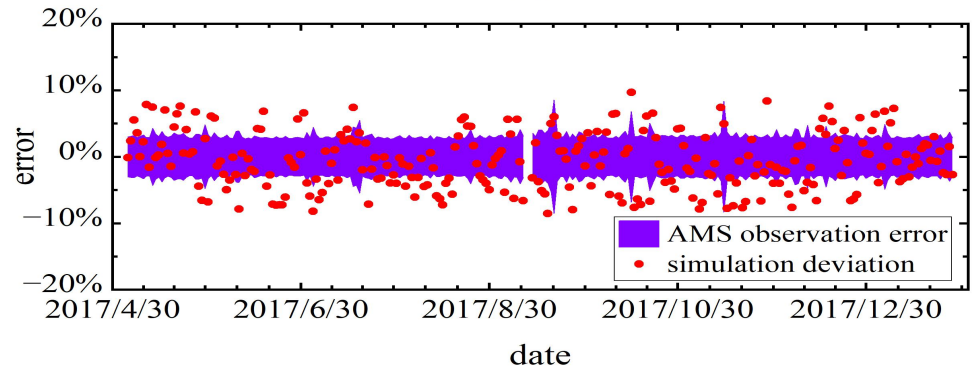
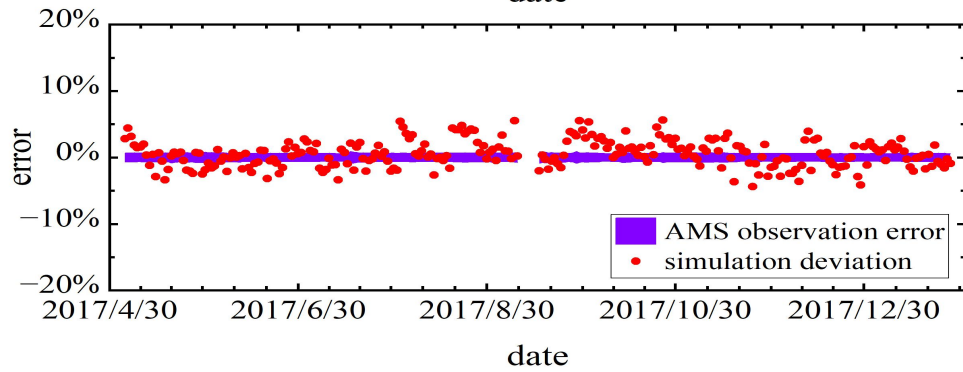
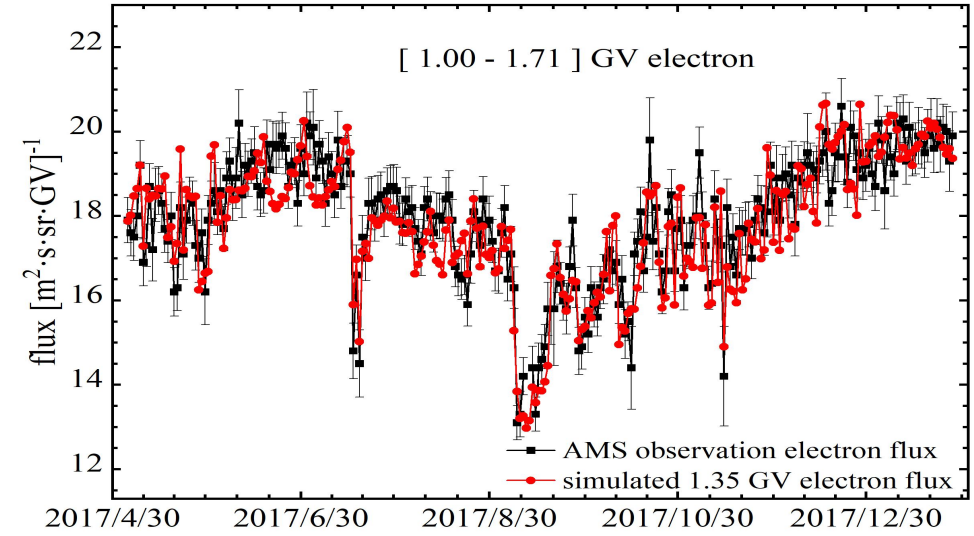
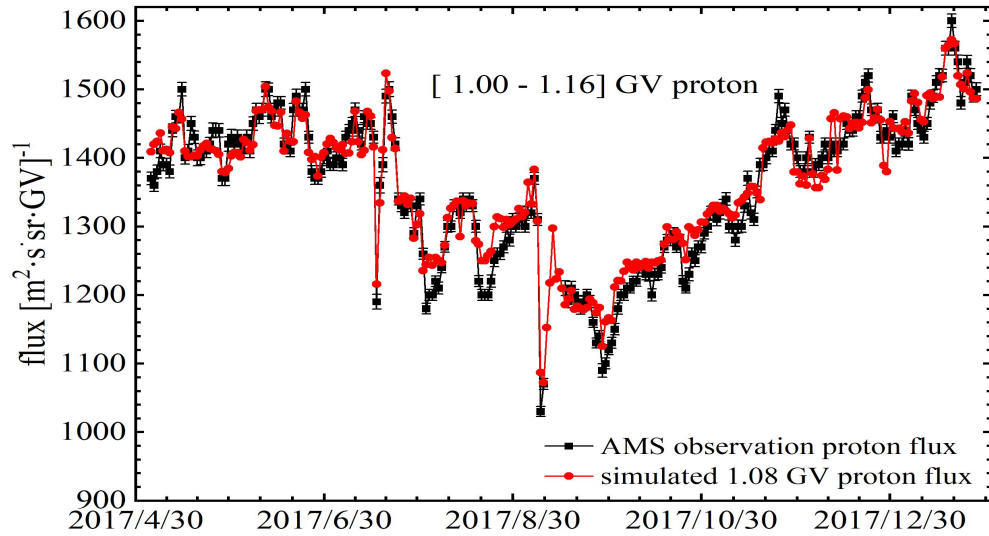


Luo+ ApJ 2011

# Global Merged Interaction Region

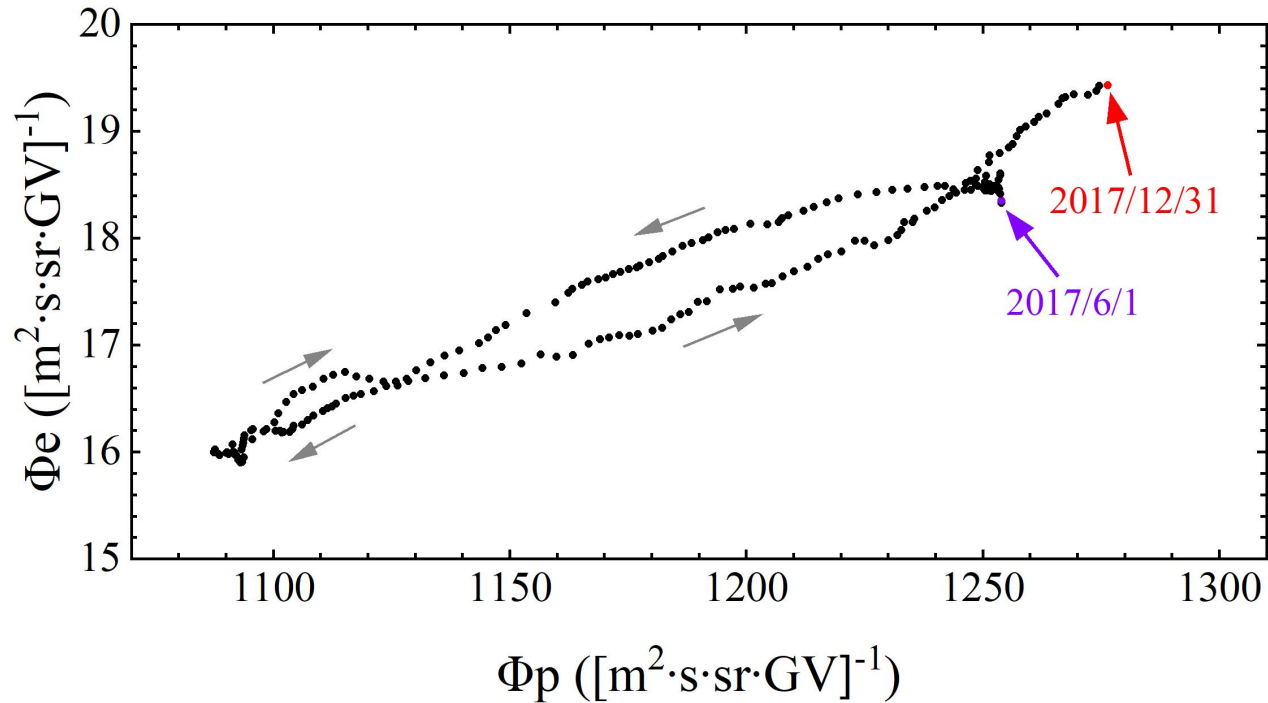


# Simulation For 2017 Decrease Event



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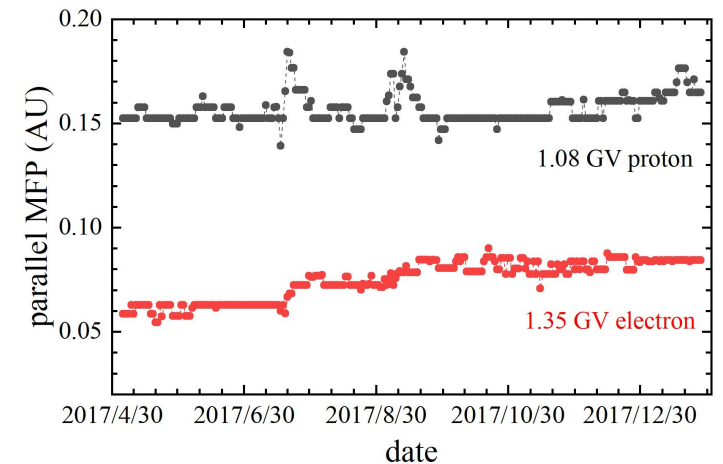
The grey arrows point in the direction of time increase.

[ 1.00 – 1.71 ] GV

$J_p$ : average of simulation results at 1.08 GV, 1.24 GV, 1.42 GV, 1.61 GV

$J_e$ : simulation results at 1.35 GV

$\Phi_p$  and  $\Phi_e$  : moving average of 2 BRs' (54 days)  $J_p$  and  $J_e$  with a step of 1 day



# Summary

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1. Based on Parker transport theory, state of art cosmic ray transport model has been developed, cosmic ray short-term solar modulation has been studied.
2. AMS GCR observation can be reproduced by the numerical model, the GCR observation during the solar magnetic field reversal period has also been reproduced.
3. Recent AMS observation provides much challenge for the current cosmic ray transport theory and numerical models.

Thanks!